

Two planes on merging routes are:

- different distances from the intersection*
- traveling at the same speed.*

Try to resolve a separation violation at the intersection with an alternate route.

SMART SKIES

Airspace Systems—Predicting Air Traffic Conflicts

Teacher Guide

Curriculum Supplement 4

Overview of Curriculum Supplement 4

You may choose to spread the experiment and calculation activities over two or three class periods, allowing time for setting up the experiment, conducting the experiment, doing the calculations, and discussing the outcomes.

This is the fourth in a series of Airspace Systems Curriculum Supplements that address distance-rate-and time problems. Each Curriculum Supplement consists of an experiment, worksheets to support the experiment, worksheets for paper-and-pencil calculations, a student analysis of the airspace scenario, and optional pre- and post-assessment instruments.

In this Curriculum Supplement, the controller must merge two flows of air traffic into one stream. The planes are each a different distance from the intersection and both are traveling at the same constant (fixed) speed. For safety reasons, when the first plane reaches the intersection, the planes must be separated by a distance greater than or equal to a given standard separation distance. If their separation is less than this standard, a separation violation will occur.

In Curriculum Supplement 3, the same given conditions resulted in a separation violation at the intersection. There are basically two ways to avoid a predicted separation violation: change the speed or change the route of one of the aircraft. The current Supplement (Curriculum Supplement 4) uses an alternate route to try to resolve the separation violation.

Given the alternate route, students must predict whether the two airplanes on intersecting paths will obey the separation standard at the new point of intersection.

Airspace Scenario

Students will determine if two airplanes traveling on different merging routes will conflict with one another at the intersection of their flight routes.

The airplanes are each a **different distance from the point of intersection**.

The airplanes are traveling at the **same constant (fixed) speeds**.

Objectives

Introducing Your Students to the Airspace Scenario

If you have not already done so, you may want to show the “Gate to Gate” CD-ROM to introduce your students to the air traffic control system. (For more detail, see the Smart Skies Airspace Systems Introduction for Teachers.)

There is also a **separation requirement**. That is, there is a requirement for a minimum distance between the planes when the first plane arrives at the point where the two routes meet.

Based upon the results of the previous Curriculum Supplement (Curriculum Supplement 3), students know that the separation standard will be violated. To try to avoid the violation, one airplane is given an **alternate route**.

Students will determine the following:

If two planes are traveling at the same constant (fixed) speed on two different routes and the planes are different distances from the point where the two routes come together, the planes will arrive at the intersection at different times.

Also, since the planes are traveling at the same constant (fixed) speed, their separation will remain the same. So at the intersection, the separation between the planes will be the same as their initial separation. Since the planes do not meet the separation standard at the start, they will not meet the separation standard at the intersection.

To resolve the separation violation, one of the planes can be redirected to an alternate route.

To help your students understand the problem, you can ask them to consider this related problem that is set in a more familiar context:

Two students, Ana and Alex, plan to meet at the movies. Ana lives 20 blocks from the theater. Alex lives 16 blocks from the theater. Ana and Alex will each leave their homes at the same time and walk at the same constant (fixed) speed.

At the last minute, Ana and Alex change their plans and decide to meet at an ice cream shop, 10 blocks beyond the original theater. Ana walks first to the theater and continues to the ice cream shop. Alex knows a shortcut to the ice cream shop and heads straight there from home without walking to the theater. His total trip is 24 blocks.

You can ask your students these questions:

Who will arrive at the ice cream shop first, Ana or Alex? Why? When the first student arrives at the ice cream shop, the other

Activity 4.0 --

Problem Statement

In a real-world scenario, each plane speed might be 400 nautical miles per hour. One plane might be 40 nautical miles from the original point of intersection. The other plane might be 36 nautical miles from that point. The separation standard might be 5 nautical miles. The alternate route might be 52 nautical miles to the new point of intersection. The new point of intersection would be 20 nautical miles beyond the original point.

An international nautical mile is 1,852 meters.

A nautical mile per hour is called a “knot”.

As a problem extension, you may want to ask your students to solve the problem using real-world data.

Student Handout:
Worksheet 4.0

student will be how many blocks away from the theater?

Problem Statement

Worksheet 4.0 describes and illustrates the airplane scenario. The speed of each airplane is 1/2 foot/second. The separation standard is 5 feet along the flight path. In particular, at the point of intersection, the planes must be at least 5 feet apart.

In the original scenario, one airplane is 20 feet from the point of intersection and the other airplane is 16 feet from the point of intersection. The alternate route results in a new point of intersection, 10 feet beyond the original point.

So one airplane is now $20 + 10 = 30$ feet from the *new* point of intersection. The alternate route is 24 feet long, so the plane on the alternate route is 24 feet from the *new* point of intersection.

Note: These speeds and distances were chosen to reflect the classroom experiment that the students will conduct and are not related to real-world parameters.

Five questions are posed:

Q1: How many seconds will it take Flight WAL27 to travel 30 feet to the *new* point where the routes come together?

Q2: How many seconds will it take Flight NAL63 to travel 24 feet to the *new* point where the routes come together?

Q3: Will the planes meet at the *new* point where the routes come together?

Q4: If not, how far apart will the planes be when the first plane reaches the *new* point where the routes come together?

Q5: Does this distance meet the separation requirement?

Since the planes are traveling at the same constant (fixed) speed and each must travel a different distance to the point of intersection, students may be able to answer Question 3 correctly without answering Questions 1 and 2. That is, they may realize that the planes will not meet.

Students may also realize that the separation distance at the new intersection will be the same as the difference in starting distances

from the new intersection. Since both planes are traveling at the same speed, they maintain the same difference in distance from the new intersection. (In this example, one plane starts 6 feet closer to the new intersection than the other plane, so the separation at the intersection will also be 6 feet.) Since this separation is greater than the 5-foot separation standard, a separation violation will *not* occur.

Materials

Worksheet 4.0: Problem Statement

Activity 4.1 --

Pretest

Estimated time:
15 - 30 minutes

The pretest is optional.

Instead of distributing the pretest, you may want to use the questions to guide a classroom discussion.

Student Handouts:
Worksheet 4.1A
Worksheet 4.1B

Pretest—Make a Prediction

The pretest steps the student through a careful reading of the airplane problem statement. The student is then asked to predict the outcome of the given airplane scenario.

The pretest may be assigned as either an individual or a small-group activity.

If your students have completed other Airspace Systems Curriculum Supplements, you may want to direct them to use a particular calculation method or methods to answer the pretest questions. In that case, Worksheet 4.1B contains blank vertical line plots as well as grids that students can use as they do their calculations.

Materials

Worksheet 4.1A: Pretest—Make A Prediction
Worksheet 4.1B: Lines and Grids

Activity 4.2 --

Experimentation

Estimated time:
Setup—30 minutes
Experiment—30 minutes

For a step-by-step student orientation to the Experiment, see Curriculum Supplement 0, the introduction to Airspace Systems.

Student Handouts:
Worksheet 4.2A
Worksheet 4.2B
Worksheet 4.2C

Classroom Experiment

In this small-group activity, students mark off the jet routes on the classroom floor or on an outdoor area. Students assume the roles of pilots, air traffic controllers, and NASA scientists. The pilots step down the jet routes at a prescribed pace. The NASA scientists track and record the pilots' times and the pilots' distances from the new intersection of the routes. The air traffic controllers set the pace and measure the separation distance when the first plane arrives at the new intersection.

Materials

Activity 4.2A: Set Up the Experiment
--sidewalk chalk or masking tape
--measuring tape or ruler

You may want to give students an overview of the experiment including an explanation of what they will do in each activity.

You may want to ask your students to compare the experiment distances and speeds with the real-world speeds given in the sidenote for Activity 4.0.

You may want to ask your students to estimate the route layout before they measure.

Students who have little experience in measurement may benefit from first practicing skip counting (by 6) to prepare them to measure 6-inch lengths.

It may be difficult for some student pilots to take 6-inch steps by placing one foot in front of the other. Instead, advise the pilots to place one foot on either side of the jet route and align their toes at each mark. It may be

--marking pens (optional)

Activity 4.2B: Conduct the Experiment

--1 stopwatch or 1 watch with a sweep second hand or 1 digital watch that indicates seconds

--pencils and Data Sheets (Worksheet 4.2C)

--signs identifying pilots, controllers, and NASA scientists

Note: the signs are available on the Smart Skies website.

--clipboard (optional)

Student Handouts:

--Worksheet 4.2A: Set Up the Experiment

--Worksheet 4.2B: Conduct the Experiment

--Worksheet 4.2C: Data Sheet

Worksheet 4.2A, Set Up the Experiment

To help students realize that the alternate route results in a new point of intersection, you may want to set up the original routes as well as the alternate route. Then note the original and the new points of intersection.

If there is not enough room to set up the two *original* routes (a 20-foot route and a 16-foot route) at right angles to one another, another angle may be used. In this case, first lay out the 10-foot segment. Then start at the bottom of the 10-foot segment and use one tape measure to lay out the 16-foot segment. At the same time, start at the top of the 10-foot segment and use a second tape measure to lay out the 24-foot segment. The three segments should form a triangle. Finally, lay out the 20-foot segment.

You may want to set up one jet route layout as a model that your students can copy.

After a group of students has completed its jet route set-up, you may find it helpful to have them compare their work with another student set-up.

Worksheet 4.2B, Conduct the Experiment

Assign students to positions on 6-8 person teams as follows:

--Lead Air Traffic Controller (1 student)

--Secondary Air Traffic Controller (1 student)

--Pilots (2 students)

--NASA Scientists, 1 or 2 for each plane (2 – 4 students)

helpful for students to practice.

After the jet routes are set up, have one group of students demonstrate the experiment while the rest of the class observes. Discuss and address any issues that may arise.

Perform the activity at least three times. Compare the results of each trial. Discuss the validity of the results.

Extensions:

1. Repeat the activity using different students as the Air Traffic Controllers, Pilots, and NASA Scientists.
2. Repeat the activity using jet routes longer than 30 feet and 24 feet, respectively. Keep the ratio of the lengths 30 : 24 (that is, 5 : 4). Increase the 5-foot separation standard using the same percent increase used for the jet route lengths. Increase the plane speed and the step size to 1 foot/second.
3. Have students draw a scale model of the experiment using real-world data. (See the sidenote for Activity 4.0).

Activity 4.3 --

Calculations

Estimated time:
15 - 30 minutes per
worksheet

Calculate the Time for Each Plane to Reach the Intersection

This activity presents six different methods students can use to determine the number of seconds for each plane to arrive at the point where their routes merge.

Each worksheet may be assigned as either an individual or a small-group activity.

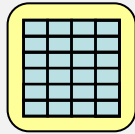
You can choose to assign one, some, or all of the worksheets. If students have completed an earlier Curriculum Supplement, you may decide to focus on only one worksheet.

You may want to assign some worksheets before and some worksheets after the experiment.

The calculation methods range in order of difficulty as follows:

- ☐ Counting (completing a table)
- ☐ Drawing blocks to make a bar graph
- ☐ Plotting points on two vertical lines
- ☐ Plotting points on a Cartesian coordinate system
- ☐ Deriving and using the distance-rate-time formula
- ☐ Graphing two linear equations

Student Handout:
Worksheet 4.3A

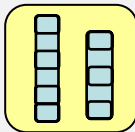


Worksheet 4.3A, Count Feet and Seconds

Students use patterns and skip-counting to complete a table and solve the problem. At the end of this activity, students may realize it is faster to multiply than to add to obtain the answer.

Prerequisite skills: count by 2s.

Student Handout:
Worksheet 4.3B



Worksheet 4.3B, Draw Blocks

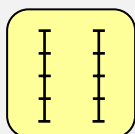
Students draw blocks, each representing the distance each plane travels in 10 seconds. The students “stack” their blocks along two vertical number lines (one line for each plane) that represent the jet routes.

Notice that the vertical lines are numbered from 30 at the bottom to 0 at the top. Students begin to stack the blocks at the starting point of each plane, 30 feet away from the *new* intersection and 24 feet away from the *new* intersection, respectively. The *new* intersection of the routes is represented with 0 at the top of each number line.

To help students make the connection between the jet routes and the vertical scales, students are first asked to plot a point on the jet route diagram and then stack the corresponding block along the vertical scale.

Prerequisite skills: read and build a bar graph with a vertical scale marked in 1-foot units; count by 10s.

Student Handout:
Worksheet 4.3C



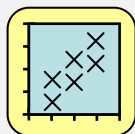
Worksheet 4.3C, Plot Points on Two Vertical Lines

This graph is similar to the way families record and compare the height of their children at the same ages. They mark off each child’s birthday height (distance from the floor) on a doorway and then record their age (time since birth) beside the height mark.

The students plot their points along two vertical number lines (one line for each plane) that represent the jet routes.

Notice that the vertical lines are numbered from 30 at the bottom to 0 at the top. The bottom of each number line corresponds to the starting point of the plane that is 30 feet away from the *new* intersection. The *new* intersection of the routes is represented with 0 at the top of each number line.

Student Handout:
Worksheet 4.3D



To help students make the connection between the jet routes and the vertical scales, students are first asked to plot a point on the jet route diagram and then plot the corresponding point on the vertical scale.

Prerequisite skills: plot a point on a (vertical) number line.

Worksheet 4.3D, Plot Points on a Cartesian Coordinate System

Notice that the vertical axis is numbered from 0 at the top to **negative** 30 at the bottom. The numbers along the vertical axis represent the distance (with a negative sign attached) from the *new* point where the two routes meet. Negative numbers are used because the points lie below the horizontal axis (the horizontal line at 0 feet).

Prerequisite skills: plot a point on a Cartesian coordinate system (the xy-plane)

Extension (optional):

For each plane, connect the points with a straight line. Find the equation of each line.

Student Handout:
Worksheet 4.3E

$$d = r \cdot t$$

Worksheet 4.3E, Derive the Distance-Rate-Time Formula

Students use patterns to derive the distance-rate-time formula in the form $d = rt$.

Prerequisite skills:
Use patterns to make a generalization.

Student Handout:
Worksheet 4.3F

$$t = d / r$$

Worksheet 4.3F, Use the Distance-Rate-Time Formula

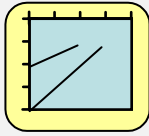
Students apply the distance-rate-time formula in the form $t = d/r$.

Prerequisite skills:
Substitute numbers into a formula.

Student Handout:
Worksheet 4.3G

Worksheet 4.3G, Graph Two Linear Equations

Notice that the points are plotted in the fourth quadrant. So the given portion of the y- axis is numbered from 0 at the top to **negative** 30 at the bottom. The numbers along the y-axis



Caution: Students may confuse the path of a plane with the graph of the plane's distance from the intersection as a function of time. In particular, students need to understand that the routes meet, but the planes do not necessarily meet.

represent the distance (with a negative sign attached) from the *new* point where the two routes meet. Negative numbers are used because the points lie below the x-axis.

Prerequisite skills:

Graph a linear equation by making a table of ordered pairs.
Find the slope of a line given the equation of the line and the graph of the line.

Extension (optional):

You may want to ask your students to find the intercepts of each line and interpret those intercepts in the context of the airspace problem.

For each plane, the y-intercept represents the plane's initial distance (with negative sign attached) from the *new* intersection point.

For each plane, the x-intercept represents the number of seconds for the plane to reach the *new* intersection point.

The horizontal distance between the x-intercepts represents the number of seconds between the arrival of the two planes at the *new* intersection.

Materials

Worksheet 4.3A: Calculate the time—count feet & seconds

Worksheet 4.3B: Calculate the time—draw blocks

Worksheet 4.3C: Calculate the time—plot on two vertical scales

Worksheet 4.3D: Calculate the time—plot points on a Cartesian coordinate system

Worksheet 4.3E: Derive the Distance-rate-time formula

Worksheet 4.3F: Use the Distance-rate-time formula

Worksheet 4.3G: Graph Two Linear Equations

Activity 4.4 --

Analysis

Estimated time:
45 minutes

Student Handout:
Worksheet 4.4

Compare the Experimental Results with the Predicted Results

Students compare the outcome of the experiment with their pretest predictions.

This activity may be assigned as either an individual or a small-group activity.

If you assigned some calculation worksheets (Activity 4.3) prior to the experiment, students can compare their calculations with the experimental results.

You may want to assign some Activity 4.3 calculation worksheets after the experiment to give students another basis for comparison.

As part of the Analysis, you may also want to ask your students to create a similar problem in a different setting. They have already considered a problem in which two students walk from their respective homes to an ice cream shop. (See the Airspace Scenario section of this document.)

Now, you might suggest they consider two cars traveling on perpendicular roads, with the two roads merging into one another. Each car is traveling at the same constant (fixed) speed. The cars are each a different distance from the merge. There is also a side road available for use by the car that is nearest the merge. Since the side road cuts the corner, students should realize it will increase the separation between the two cars when they arrive at the *new* merge.

Students may also realize that the separation distance at the new merge will be the same as the difference in starting distances from the new merge. Since both cars are traveling at the same speed, they maintain the same difference in distance from the new merge. (For example, if one car starts 6 feet closer to the new merge than the other car, the separation at the new merge will also be 6 feet.)

Note: To be consistent with the airspace scenarios, it is important that for each problem created by you or your students, you choose a fixed (constant) speed for each vehicle or person. (For example, a rocket launch scenario would *not* be appropriate because a launched rocket typically accelerates and therefore its speed is not constant.)

Materials

Worksheet 4.4: After the Experiment

Activity 4.5 --

Posttest

Estimated time:
15 - 30 minutes

*The posttest is **optional**.*

Student Handouts:
Worksheet 4.5
Worksheet 4.1B

Curriculum Supplement Posttest

This activity may be assigned as either an individual or a small-group activity.

You can direct your students to use a particular calculation method or methods to answer the posttest questions. Worksheet 4.1B (used for the Pretest) contains blank vertical line plots and grids that students can use as they do their calculations.

Materials

Worksheet 4.5: Posttest

Worksheet 4.1B: Lines and Grids



Name _____

Problem Statement

In the picture below, two airplanes are flying on different routes.

The World Airlines plane has flight number **WAL27**.

The speed of Flight WAL27 is 1/2 foot/second (0.15 meters/second).

The National Airlines plane has flight number **NAL63**.

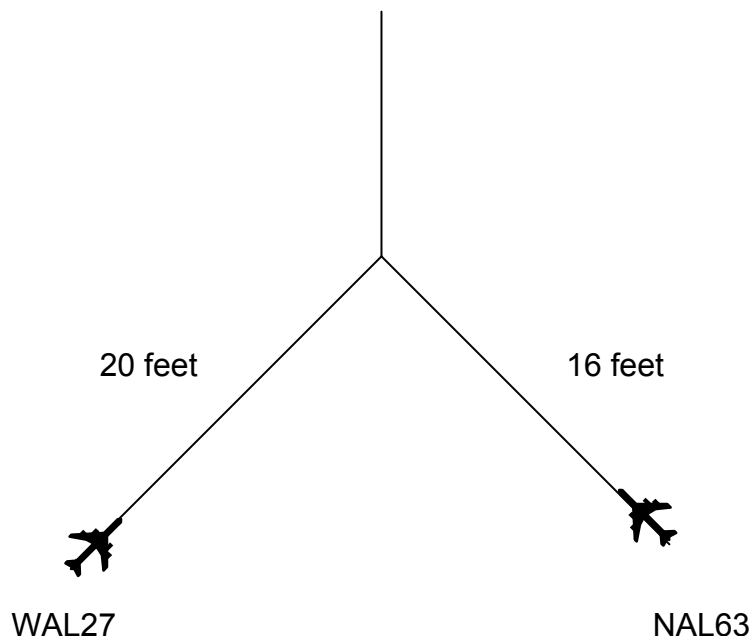
The speed of Flight NAL63 is 1/2 foot/second (0.15 meters/second).

Flight WAL27 is 20 feet (6.1 meters) away from the point where the two routes come together.

Flight NAL63 is 16 feet (4.9 meters) away from the point where the two routes come together.

To keep the pilots and passengers safe, the planes must be at least 5 feet (1.5 meters) apart when the first plane reaches the point where the routes come together. If the distance between the planes is less than 5 feet, then it may not be safe.

This 5-foot distance is called a *separation standard*.





Name _____

In another experiment (Curriculum Supplement 3), you learned that the planes would **not** meet the separation standard. That is, they will be closer than 5 feet (1.5 meters) when the first plane arrives at the point where the routes come together.

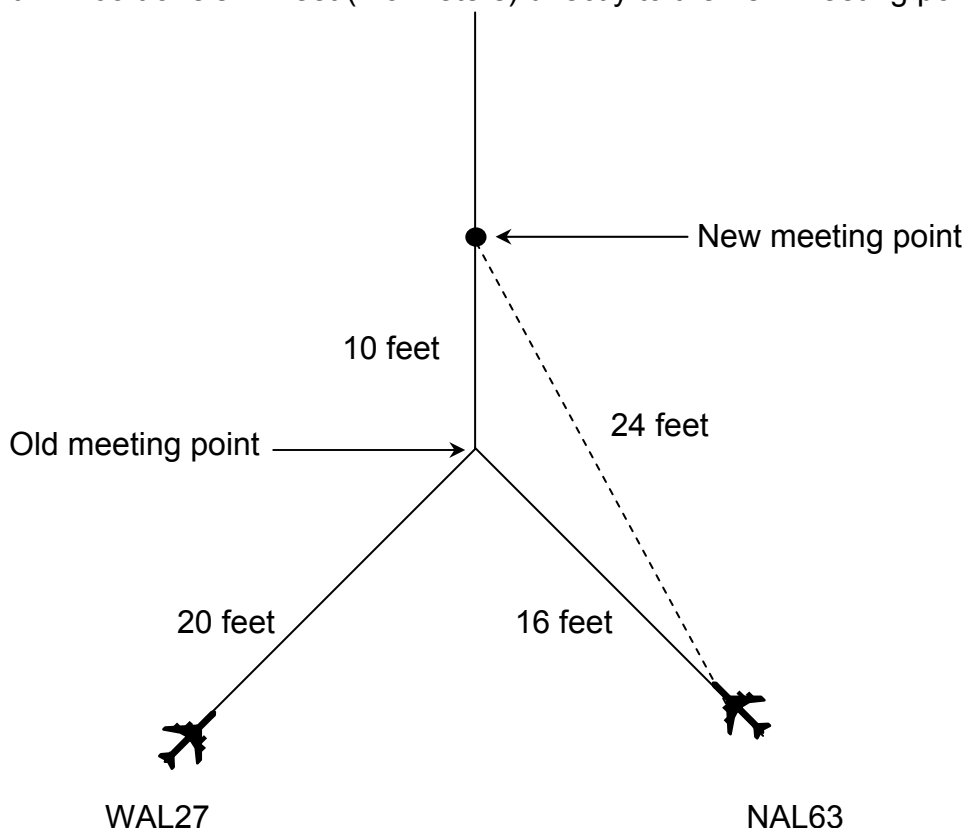
To solve this problem, the air traffic controllers give Flight NAL63 a new, longer route. The new route is 24 feet (7.3 meters) long. The new route is shown with a dotted line.

The new route for Flight NAL63 and the old route for Flight WAL27 come together in a **new** meeting point.

Flight WAL27 follows its old route for 20 feet (6.1 meters) until it reaches the old meeting point.

Then it turns and keeps going 10 feet (3.0 meters) to the new meeting point.

Flight NAL63 travels 24 feet (7.3 meters) directly to the new meeting point.





Name

Question 1: How many seconds will it take Flight WAL27 to travel 30 feet to the **new** point where the two routes come together?

Question 2: How many seconds will it take Flight NAL63 to travel 24 feet to the **new** point where the two routes come together?

Question 3: Will the planes meet at the **new** point where the two routes come together?

Question 4: If not, how many feet apart will the planes be when the first plane reaches the **new** point where the routes come together?

Question 5: In Question 4, does the distance meet the 5-foot separation standard?



Name

Pretest—Make a Prediction

The picture on the next page shows two airplanes and three jet routes.

The World Airlines plane has flight number WAL27.

Use your pencil to trace the route for Flight WAL27.

Start at the picture of the plane and move 20 feet to the old meeting point.

Then turn and move 10 feet to the new meeting point.

1. How many feet will Flight WAL27 travel to the new meeting point? _____

The speed of Flight WAL27 is $\frac{1}{2}$ foot/second.

2. Write the speed of Flight WAL27 next to its picture.

3. How far does Flight WAL27 travel in one second? _____

The National Airlines plane has flight number NAL63.

Use your pencil to trace the route for Flight NAL63.

Start at the picture of the plane and move 24 feet **on the dotted line**
to the new meeting point.

The speed of Flight NAL63 is $\frac{1}{2}$ foot/second.

4. Write the speed of Flight NAL63 next to its picture.

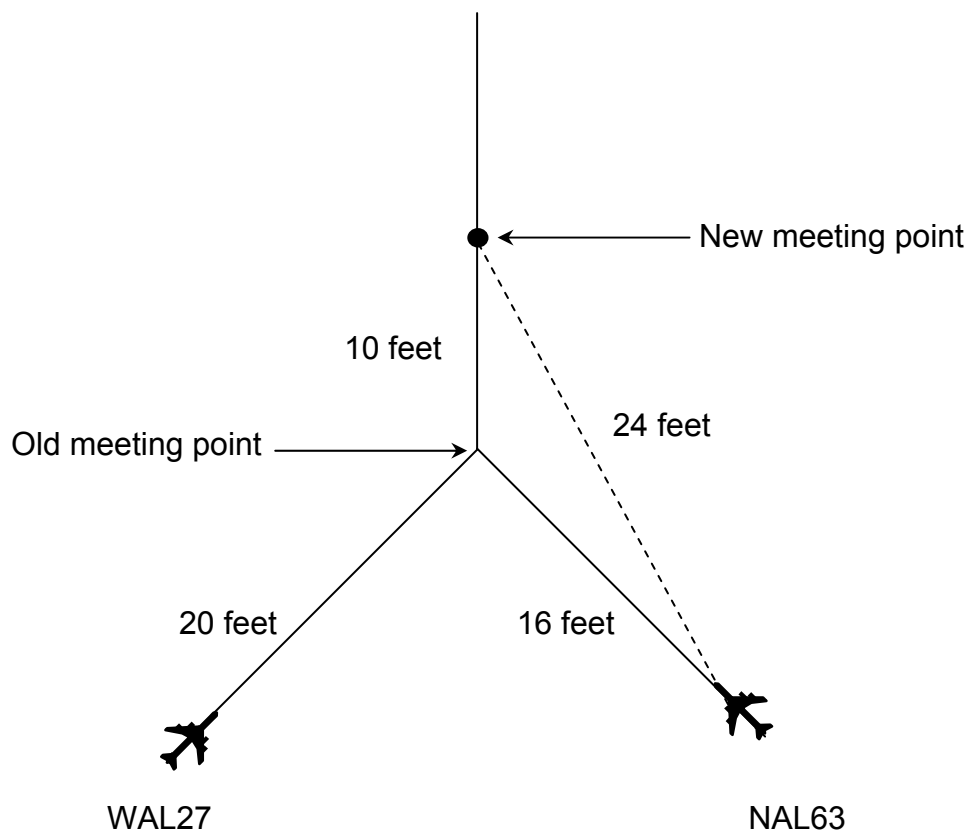
5. How far does Flight NAL63 travel in one second? _____



Name

6. Do you think that the two planes will meet at the **new** point where the two routes come together? _____
Why or why not? _____

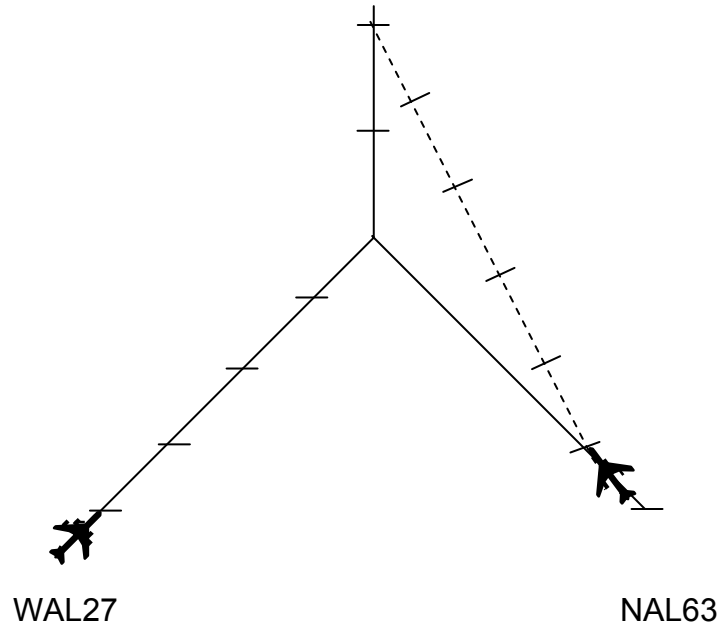
7. If not, how many feet apart do you think the planes will be when the first plane reaches the point where the routes come together? _____
8. Does your answer to Question 7 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? _____





Name

Lines and Grids



Distance
from
the point
where the
routes meet

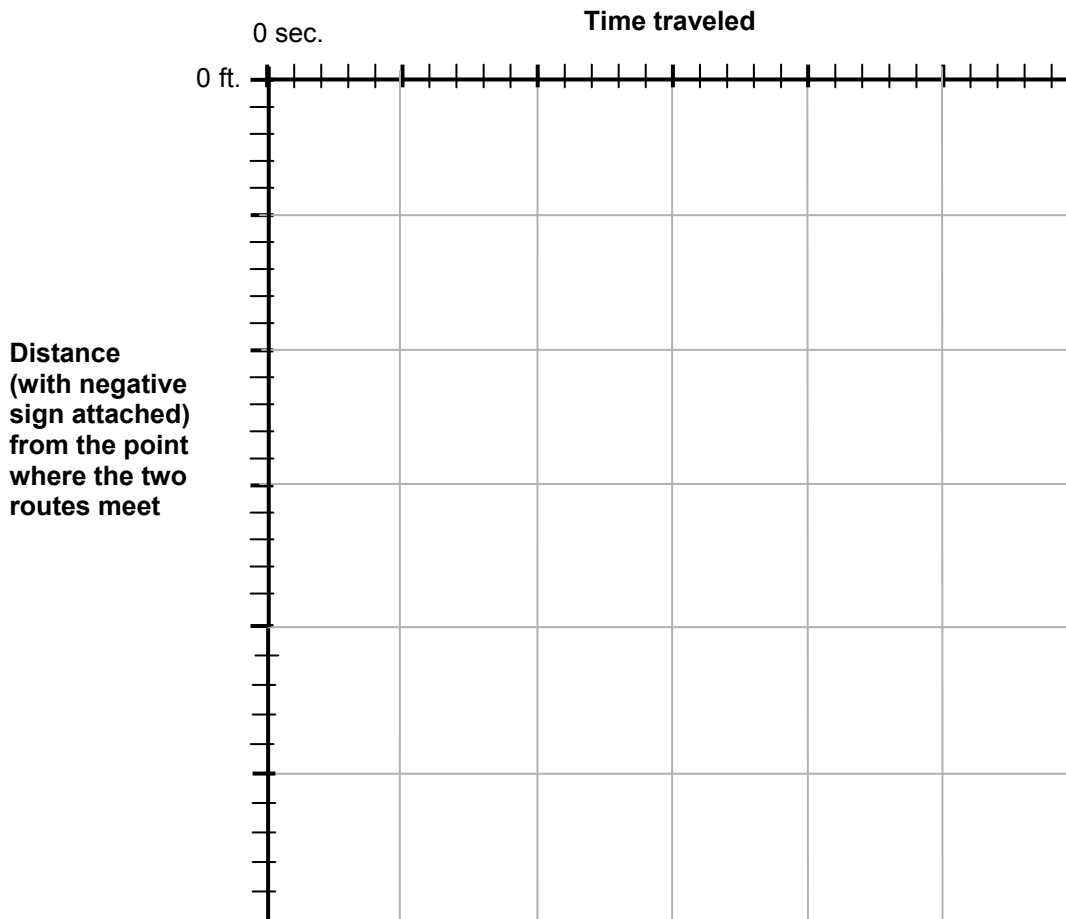
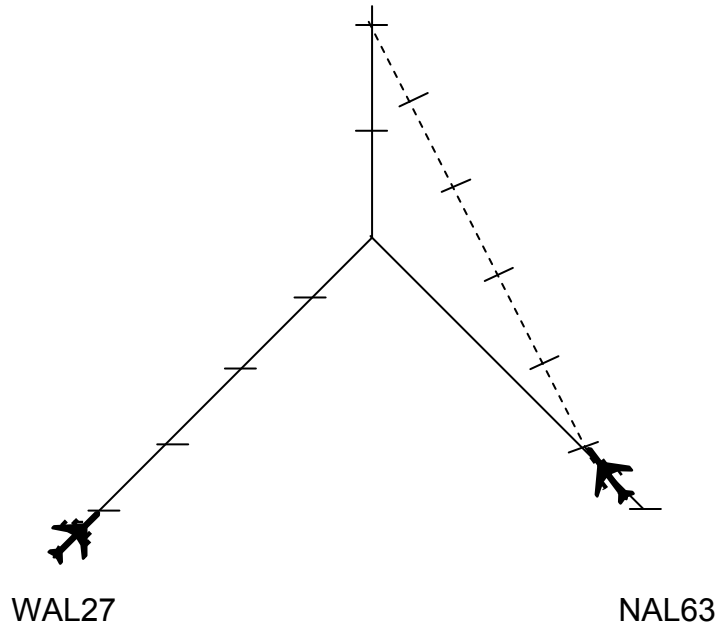
0 ft.

0 ft.



Name

Lines and Grids





Name _____

Set Up the Experiment

1. Use sidewalk chalk (or masking tape) to lay out four jet route segments as shown on page 2. Lay out the four jet route segments in this order:

- ☐ First, lay out the 10-foot segment.
- ☐ Next, start at the bottom of the 10-foot segment and use one tape measure to lay out the 16-foot segment. At the same time, start at the top of the 10-foot segment and use a second tape measure to lay out the 24-foot segment. The three segments should form a triangle.
- ☐ Finally, lay out the 20-foot segment.

When you are done, check your measurements as follows:

The route for WAL27 should be 30 feet long (20 feet plus 10 feet).

The route for NAL63 should be 24 feet long.

2. The speed of each plane is $\frac{1}{2}$ foot/second.

- ☐ Stand at the beginning of the 20-foot segment. Place a mark (or a piece of masking tape) every $\frac{1}{2}$ foot (every 6 inches) along the segment.
- ☐ Stand at the beginning of the 10-foot segment. Place a mark (or a piece of masking tape) every $\frac{1}{2}$ foot (every 6 inches) along the segment.
- ☐ Stand at the beginning of the 24-foot segment. Place a mark (or a piece of masking tape) every $\frac{1}{2}$ foot (every 6 inches) along the segment.

These marks will guide the pilots as they step down the jet route segments.

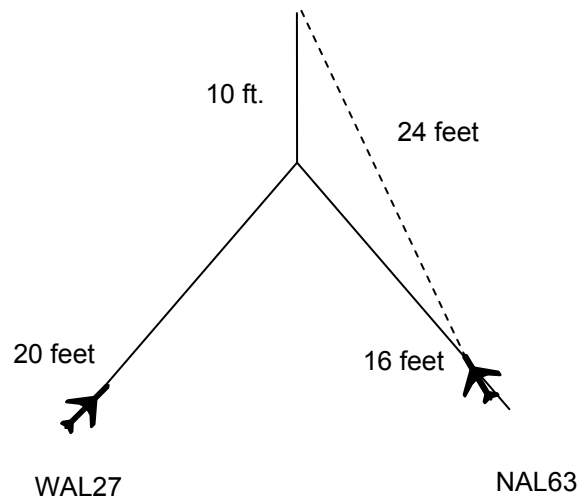
Note: You do *not* need to place marks or tape along the 16-foot segment since the NAL63 pilot will use only the 24-foot segment.



Name

3. On the 30-foot jet route for WAL27, place and label mark a longer chalk mark (or piece of masking tape) at the following positions:
5 feet from the start, **10 feet** from the start, **15 feet** from the start,
20 feet from the start, **25 feet** from the start, the **finish point**.
4. On the 24-foot jet route for NAL63, place and label mark a longer chalk mark (or piece of masking tape) at the following positions:
5 feet from the start, **10 feet** from the start, **15 feet** from the start,
20 feet from the start, the **finish point**

Note: The finish point is the **new** point where the jet routes meet.





Name

Conduct the Experiment

1. Review your prediction.

Do you think the airplanes will meet at the new point where the two routes meet?"

Why or why not? If not, how many feet apart do you think the planes will be when the first plane reaches the new point where the routes come together?

2. Take your position. Circle your role in the diagram and in the following list:

Lead Air Traffic Controller: Give the command "Take your ready positions."

Pilots: Position yourself at the start of your jet route.

Secondary Controller: Take your data sheet, measuring tape, and pencil and go to your controller location as shown below.

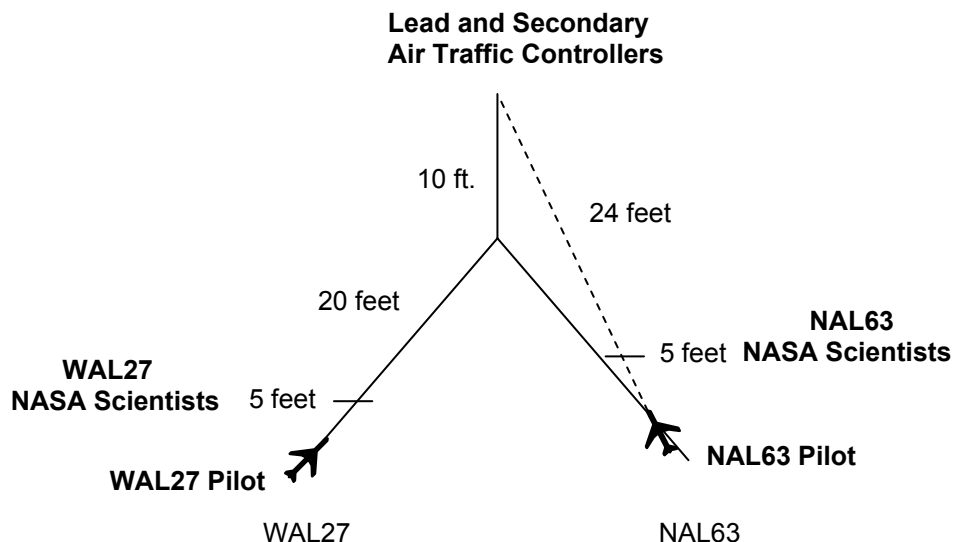
NASA Scientists: Take your data sheet and pencil and go to your first observation position at the 5-foot line as shown below.

3. Get ready to begin. Circle your role in the following list:

Lead Air Traffic Controller: Give the command "Set."

Pilots: Prepare to step down your jet route. You may want to practice first. It helps to keep one foot on each side of the jet route.

NASA Scientists: Get ready to measure and record the information on the data sheet.





Name

4. Begin the experiment. Circle your role in the following list:

Lead Air Traffic Controller: Give the command “Ready.” Start your stopwatch and count the seconds aloud, “One, two, three...” and so on.

Pilots: Take your first step on count “One.” Each second, take one step to the next timing mark.

NASA Scientists: Record the time your aircraft arrives at the 5-foot line. Stay ahead of the pilot and record the time your aircraft arrives at the 10-foot line, the 15-foot line, the 20 foot line, the 25 foot line (for flight WAL27), and the point where the Controller says, “Halt.”

5. End the experiment. Circle your role in the following list:

Secondary Controller: When the first Pilot reaches the new point where the two routes meet, give the command “Halt.” Measure and record the separation distance between the planes. To do this, measure the distance of the second Pilot from the new point where the two routes meet.

Lead Air Traffic Controller: Stop counting the seconds when you hear “Halt.”

Pilots: Stop and remain where you are on the jet route when you hear “Halt.”

NASA Scientists: Record the “Halt” time.



Name

Data Sheet

a. Fill in this table:

Flight Number	Speed	Distance from the Point Where the Two Routes Meet
WAL27		
NAL63		

b. On the picture below, circle your job title. Notice the data you need to record.

c. During Experiments 1, 2, and 3, record your data.

1	2	3

**Separation Distance (feet)
at New Intersection**

1	2	3

Air Traffic Controllers

"HALT" Time

1	2	3

"HALT" Time

1	2	3

Time (seconds)

1	2	3

Time (seconds)

1	2	3

Time (seconds)

1	2	3

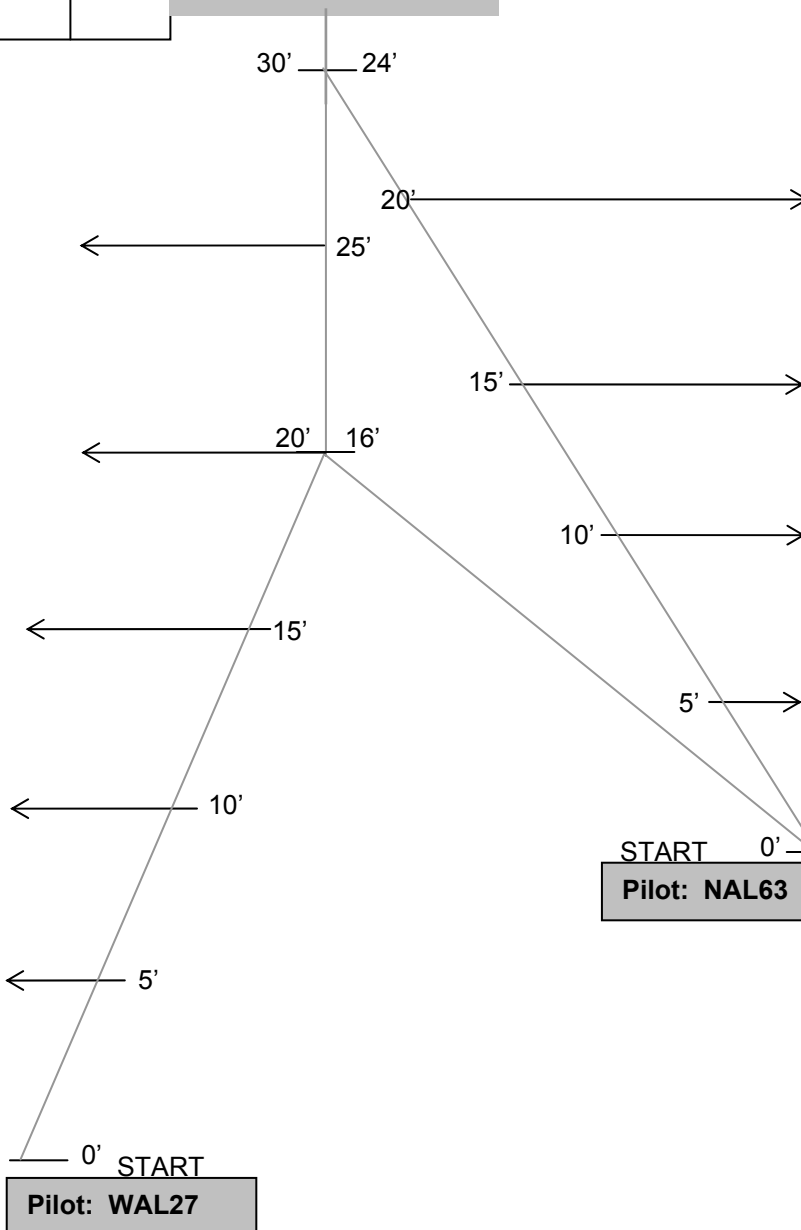
Time (seconds)

1	2	3

Time (seconds)

1	2	3

NASA Scientist: WAL27
Start recording here.



Time (seconds)

1	2	3

Time (seconds)

1	2	3

Time (seconds)

1	2	3

Time (seconds)

1	2	3

NASA Scientist: NAL63
Start recording here.

START 0'
Pilot: NAL63

0' START
Pilot: WAL27



PILOT



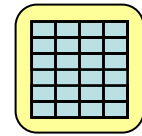
AIR TRAFFIC CONTROLLER

NASA SCIENTIST





Name



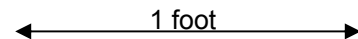
How Much Time To Reach the Point Where the Two Routes Meet?
(Count Feet and Seconds to Find the Answer)

The speed of each airplane is $\frac{1}{2}$ foot per second.

That means each airplane travels $\frac{1}{2}$ foot in 1 second.



So each airplane travels 1 foot in 2 seconds.



Flight WAL27 starts 30 feet from the **new** point where the two routes meet.

Flight NAL63 starts 24 feet from the **new** point where the two routes meet.

1. Fill in the given table to see how many seconds it will take each plane to travel to the new point where the two routes meet.

After you fill in the table, answer the following questions:

2. How many seconds will it take each plane to arrive at the new point where the two routes meet?

WAL27 _____ seconds

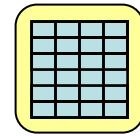
NAL63 _____ seconds

3. Will the two planes meet at the new point where the two routes come together? _____

4. Why or why not? _____



Name

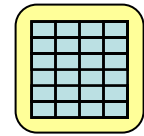


5. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the new point where the routes come together? _____
6. Does your answer to Question 5 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the new point where the routes come together? _____
7. You filled in the table to find the answers. Can you think of a faster way to find the answer? If so, describe the faster way. _____

8. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____



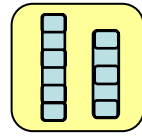
Name



Flight WAL27		Flight NAL63	
How many feet?	How many seconds?	How many feet?	How many seconds?
1	2	1	2
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			
16			
17			
18			
19			
20			
21			
22			
23			
24			
25			
26			
27			
28			
29			
30			



Name



How Much Time To Reach the Point Where the Two Routes Meet?
(Draw Blocks to Find the Answer)

Flight WAL27 starts 30 feet from the **new** point where the two routes meet.

Flight NAL63 starts 24 feet from the **new** point where the two routes meet.

The speed of each airplane is $\frac{1}{2}$ foot per second.

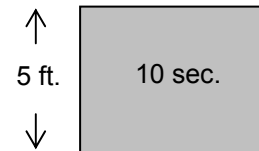
In 1 second, each airplane travels $\frac{1}{2}$ foot.

In 2 seconds, each airplane travels 1 foot.

In 10 seconds (5×2 seconds), each plane travels 5×1 foot.

That is, each plane travels 5 feet in 10 seconds.

The height of this block represents 5 feet, the distance each plane travels in 10 seconds.



Now you will use blocks and dots to plot the position of each plane as it travels to the new point where the two routes meet.

Look at the top picture on page 4. It shows the two jet routes.

Flight NAL63 started 24 feet away from the new point where the two routes meet.

After 10 seconds, Flight NAL63 has moved 5 feet closer to that point.

So the plane is 19 feet from the point where the two routes meet.

A dot shows the position of Flight NAL63 after 10 seconds.

Flight WAL27 started 30 feet away from the new point where the two routes meet.

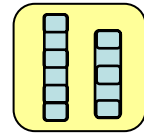
After 10 seconds, Flight WAL27 has moved 5 feet closer to that point.

So the plane is 25 feet from the point where the two routes meet.

A dot shows the position of Flight WAL27 after 10 seconds.



Name _____



The dots are connected with a line marked “10 seconds.”

Next look at the bottom picture on page 4. It shows a bar graph made of blocks.

A block shows the position of Flight NAL63 after 10 seconds.

A block shows the position of Flight WAL27 after 10 seconds.

The blocks are connected with a line marked “10 seconds.”

Now it's your turn to draw and connect.

- ☐ On the top picture on page 4, draw a dot to show the position of Flight NAL63 after 20 seconds.
- ☐ On the bottom picture on page 4, trace the block that shows the position of Flight NAL63 after 20 seconds.

- ☐ On the top picture, draw a dot to show the position of Flight WAL27 after 20 seconds.
- ☐ On the bottom picture, trace the block that shows the position of Flight WAL27 after 20 seconds.

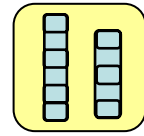
- ☐ Connect your dots with a line marked “20 seconds.”
- ☐ Connect your blocks with a line marked “20 seconds.”

- ☐ Draw and connect dots at 30 seconds.
- ☐ Draw and connect blocks at 30 seconds.

- ☐ Keep going until the first plane reaches the **new** place where the two routes meet.



Name



When you are done, answer these questions.

1. Circle the flight number of the first plane to arrive at the new point where the two routes meet. How many seconds will it take that plane to arrive at the new point where the two routes meet?

WAL27 _____ seconds

NAL63 _____ seconds

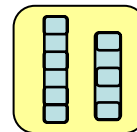
2. Will the two planes meet at the new point where the two routes come together? _____

3. Why or why not? _____

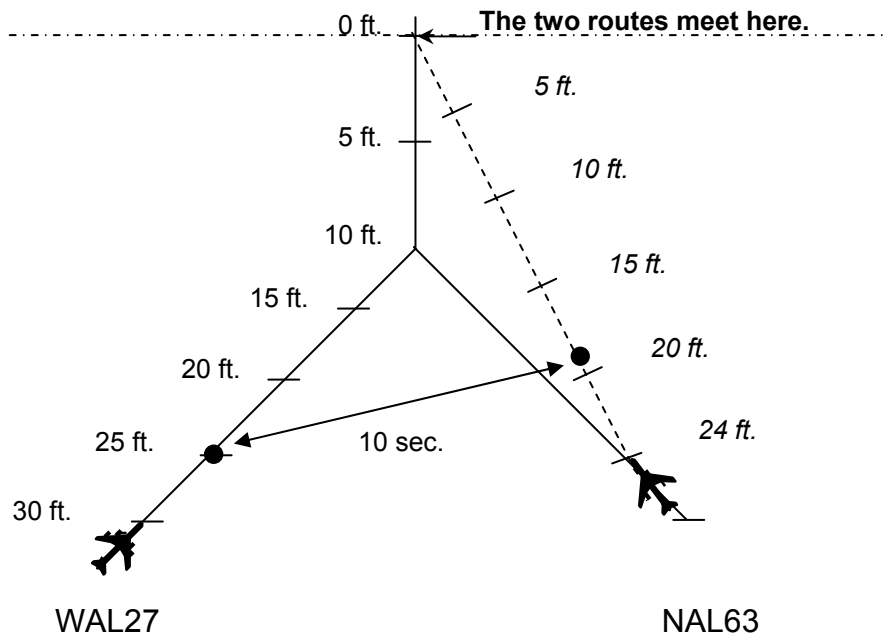
4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the new point where the routes come together? _____

5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the new point where the routes come together? _____

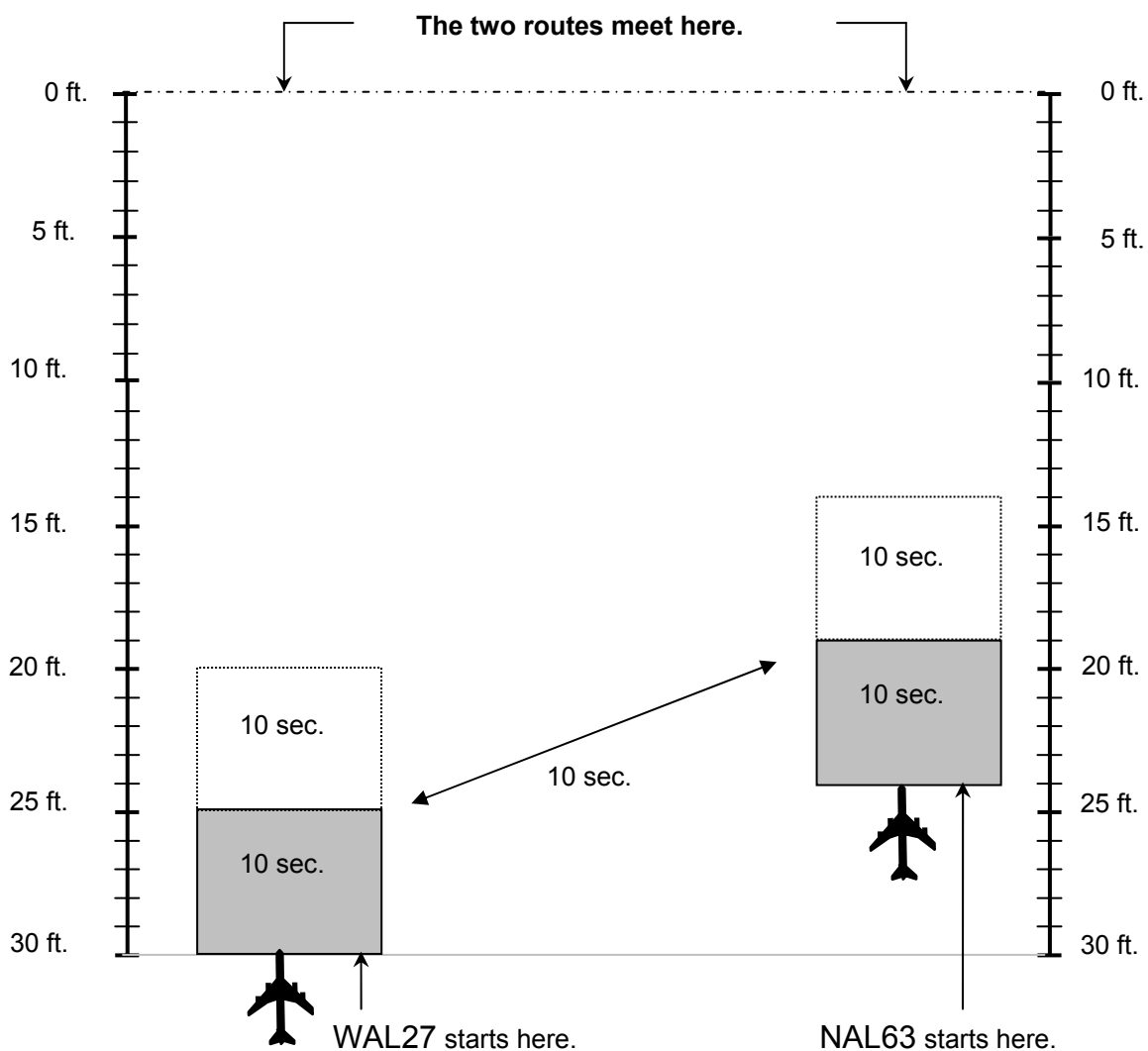
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____



Name _____

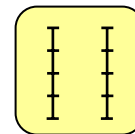


Distance
from
the new
point where
the routes
meet





Name _____



How Much Time To Reach the Point Where the Two Routes Meet?
(Plot Points on Lines to Find the Answer)

Flight WAL 27 starts 30 feet from the **new** point where the two routes meet.

Flight NAL63 starts 24 feet from the **new** point where the two routes meet.

The speed of each airplane is $\frac{1}{2}$ foot per second.

In 1 second, each airplane travels $\frac{1}{2}$ foot.

In 2 seconds, each airplane travels 1 foot.

In 10 seconds (5×2 seconds), each plane travels 5×1 foot.

That is, each plane travels 5 feet in 10 seconds.

You will use an **O** to show the position of Flight NAL63.

You will use an **X** to show the position of Flight WAL27.

Look at the top picture on page 4. The picture shows the two jet routes.

Flight NAL63 started 24 feet away from the new point where the two routes meet.

After 10 seconds, Flight NAL63 has moved 5 feet closer to that point.

So the plane is 19 feet from the new point where the two routes meet.

An **O** shows the position of Flight NAL63 after 10 seconds.

Flight WAL27 started 30 feet away from the new point where the two routes meet.

After 10 seconds, Flight WAL27 has moved 5 feet closer to that point.

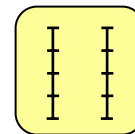
So the plane is 25 feet from the new point where the two routes meet.

An **X** shows the position of Flight WAL27 after 10 seconds.

The **X** and **O** are connected with a line marked “10 seconds.”



Name



Next look at the bottom picture on page 4. It shows two vertical line graphs.

An **O** shows the position of Flight NAL63 after 10 seconds.

An **X** shows the position of Flight WAL27 after 10 seconds.

The **X** and **O** are connected with a line marked “10 seconds.”

Now it's your turn to draw and connect.

- ☐ On the top picture on page 4, draw an **O** to show the position of Flight NAL63 after 20 seconds.
- ☐ On the bottom picture on page 4, draw an **O** to show the position of Flight NAL63 after 20 seconds.

- ☐ On the top picture, draw an **X** to show the position of Flight WAL27 after 20 seconds.
- ☐ On the bottom picture, draw an **X** to show the position of Flight WAL27 after 20 seconds.

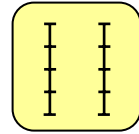
- ☐ On the top picture, connect the **X** and **O** with a line marked “20 seconds.”
- ☐ On the bottom picture, do the same thing.

- ☐ On the top picture, draw and connect an **X** and an **O** at 30 seconds.
- ☐ On the bottom picture, do the same thing.

- ☐ Keep going until the first plane reaches the **new** place where the two routes meet.



Name



When you are done, answer these questions.

1. Circle the flight number of the first plane to arrive at the new point where the two routes meet. How many seconds will it take that plane to arrive at the new point where the two routes meet?

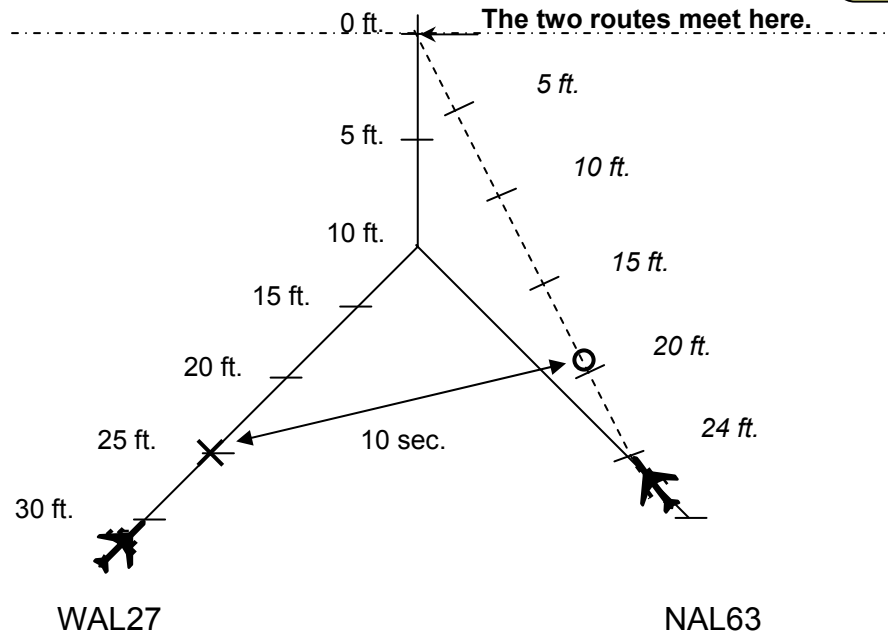
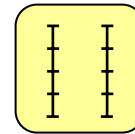
WAL27 _____ seconds

NAL63 _____ seconds

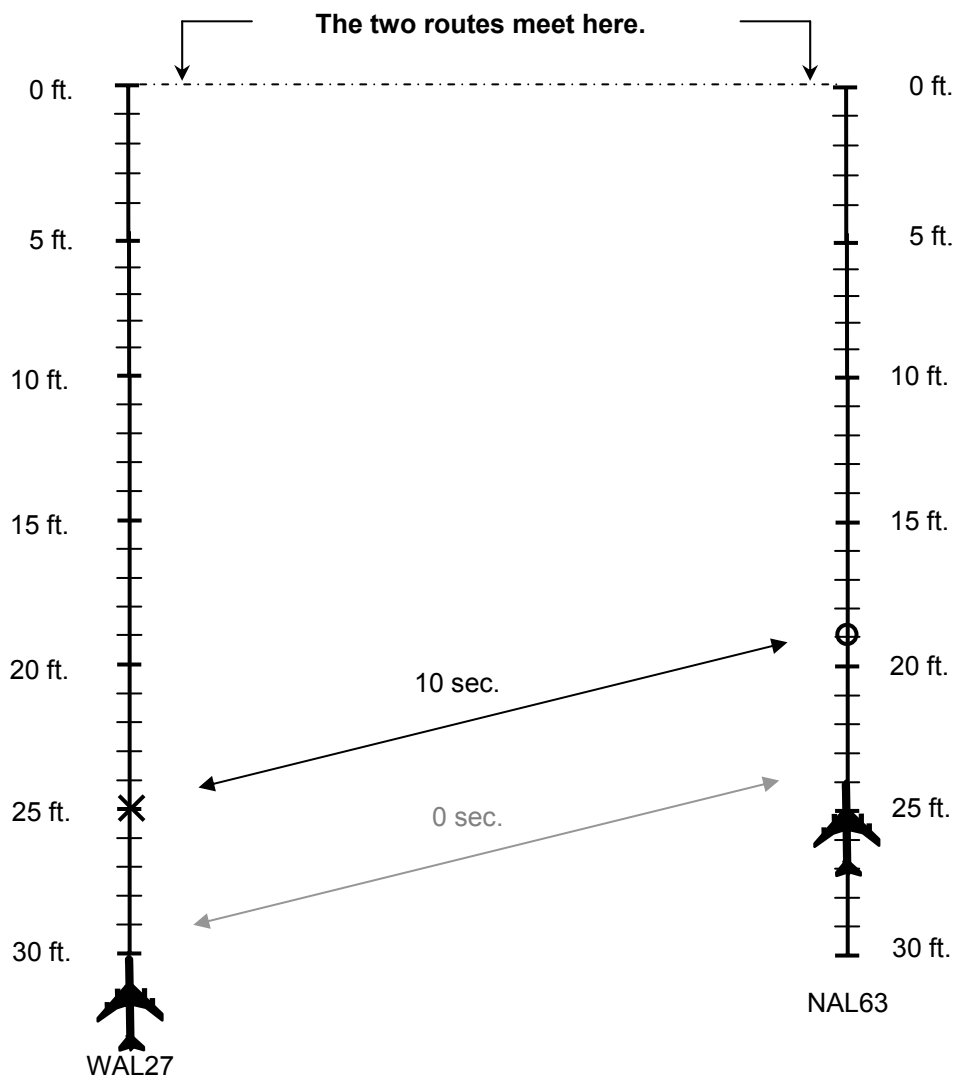
2. Will the two planes meet at the new point where the two routes come together? _____
3. Why or why not? _____
4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the new point where the routes come together? _____
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the new point where the routes come together? _____
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____



Name _____

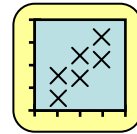


Distance
from
the point
where the
routes meet





Name _____



How Much Time To Reach the Point Where the Routes Meet? (Plot Points on a Grid to Find the Answer)

The speed of each airplane is $\frac{1}{2}$ foot per second.

In 2 seconds, each airplane travels 1 foot.

In 10 seconds, each plane travels 5 feet.

Flight NAL63 starts 24 feet from the **new** point where the two routes meet.

After 10 seconds, the plane has traveled 5 feet.

So after **10** seconds, Flight NAL63 is **19** feet **from** the point where the two routes meet.

On the NAL63 jet route on page 4, we represent that information with an **O** at 19 feet and an arrow labeled “10 seconds.”

On the grid on page 4, we represent that information with the point **(10, -19)**.

We use **negative** nineteen because the point lies **below** the horizontal line at 0 feet where the two routes meet.

The **O** at the point (10, -19) shows the position of Flight NAL63 after 10 seconds.

Flight WAL27 starts 30 feet from the **new** point where the two routes meet.

After 10 seconds, the plane has traveled 5 feet.

So after **10** seconds, Flight WAL27 is **25** feet **from** the new point where the two routes meet.

On the WAL27 jet route, we represent that information with an **X** at 25 feet and an arrow labeled “10 seconds.”

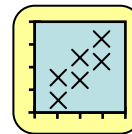
On the grid, we represent that information with the point **(10, -25)**.

We use **negative** twenty five because the point lies **below** the horizontal line at 0 feet where the two routes meet.

The **X** at the point (10, -25) shows the position of Flight WAL27 after 10 seconds.



Name



Now it's your turn to plot and connect points on the routes and to plot points on the grid on page 4.

Put an **X** at the point that shows the position of Flight WAL27 after 20 seconds, 30 seconds, and so on.

Put an **O** at the point that shows the position of Flight NAL63 after 20 seconds, 30 seconds and so on.

Keep going until the first plane reaches the horizontal line at 0 ft.
That line represents the point where the two routes meet.

When you have finished plotting points, answer these questions.

1. Circle the flight number of the first plane to arrive at the new point where the two routes meet. How many seconds will it take that plane to arrive at the new point where the two routes meet?

WAL27 _____ seconds

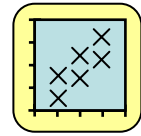
NAL63 _____ seconds

2. Will the two planes meet at the new point where the two routes come together? _____

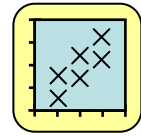
3. Why or why not? _____



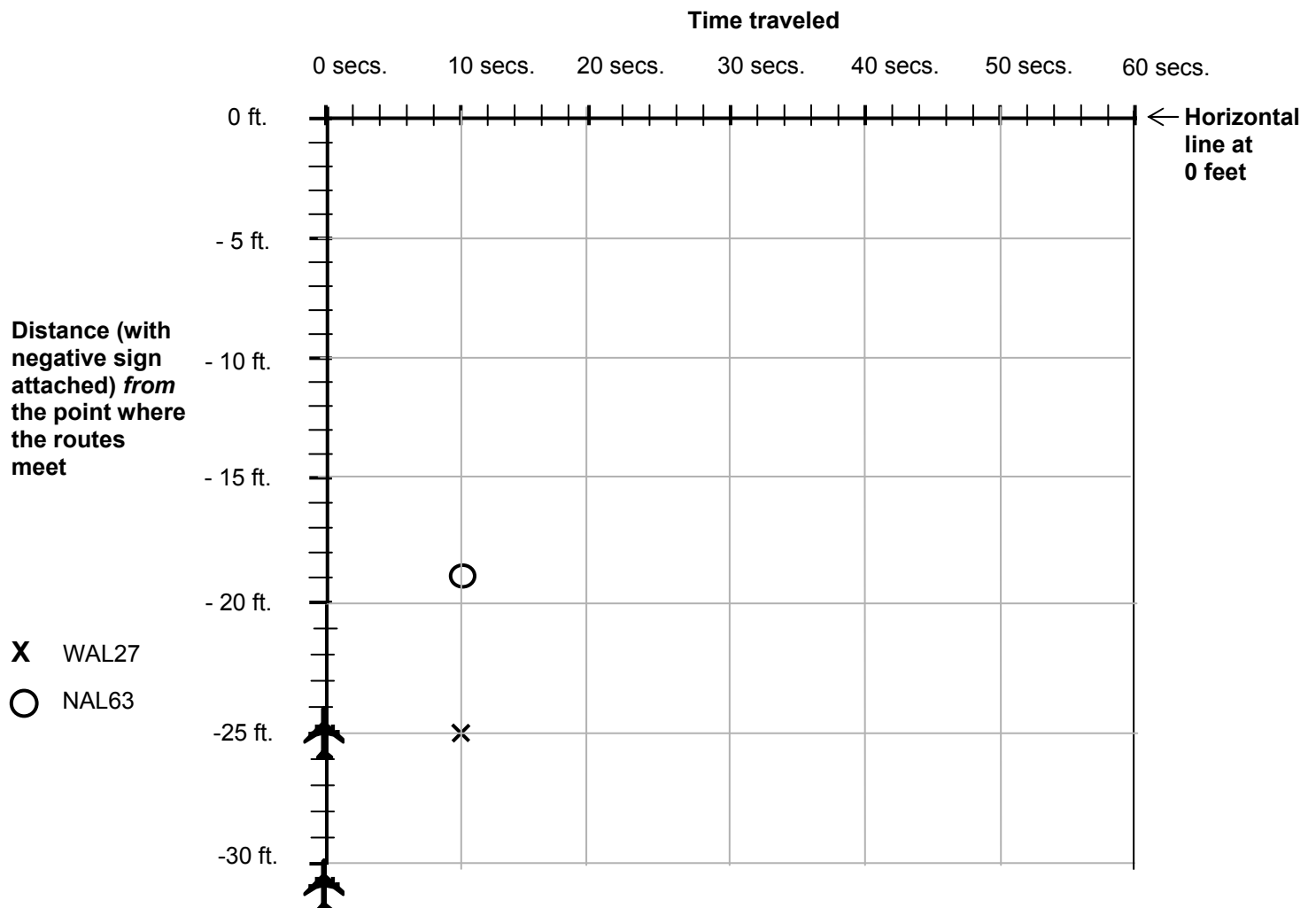
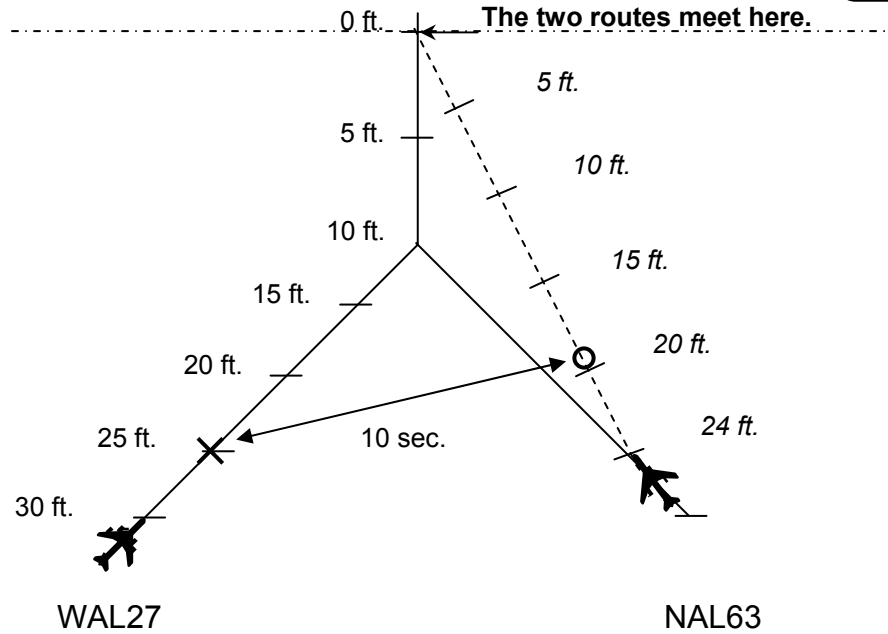
Name



4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the new point where the routes come together? _____
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the new point where the routes come together? _____
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____



Name _____





Name

$$d = r \cdot t$$

Derive the Distance-Rate-Time Formula

The speed of each airplane is 0.5 feet per second.

In 1 second, each plane travels 0.5 feet.

In 2 seconds, each plane travels $0.5 \text{ feet/second} \times 2 \text{ seconds} = 1.0 \text{ foot}$.

In 3 seconds, each plane travels $0.5 \text{ feet/second} \times 3 \text{ seconds} = 1.5 \text{ feet}$.

1. In 4 seconds, each plane travels _____ \times _____ = _____ feet.
2. In 5 seconds, each plane travels _____ \times _____ = _____ feet.
3. In 6 seconds, each plane travels _____ \times _____ = _____ feet.
4. How could you use multiplication to find the distance each plane travels in 14 seconds?

One way to find the distance is to multiply the plane's speed by 14 seconds, like this:

$$0.5 \text{ feet/second} \times 14 \text{ seconds} = 7 \text{ feet}$$

This suggests the following rule:

To find the distance traveled, multiply the speed by the time traveled.

In mathematics and science, we often say "rate" instead of "speed."

Then we can write the rule like this:

$$\text{distance} = \text{rate} \times \text{time}$$

This relationship is called the Distance-Rate-Time Formula. We often write it like this:

$$d = r \cdot t$$

5. Use the formula to find the distance traveled by each plane in 20 seconds.
In 20 seconds, each plane travels _____ feet.



Name

$$t = d / r$$

Use the Distance-Rate-Time Formula

The speed of each airplane is 0.5 feet per second.

In 1 second, each plane travels 0.5 feet.

In 2 seconds, each plane travels $0.5 \text{ feet/second} \times 2 \text{ seconds} = 1.0 \text{ foot}$.

In 3 seconds, each plane travels $0.5 \text{ feet/second} \times 3 \text{ seconds} = 1.5 \text{ feet}$.

To find the distance traveled after t seconds, we multiply the rate by the time:

$$\text{distance traveled} = \text{rate of travel} \times \text{time traveled}$$

This relationship is called the Distance-Rate-Time Formula. We often write it like this:

$$d = r \cdot t$$

If we divide both sides of this equation by r , we get a formula for time traveled:

$$t = \frac{d}{r}$$

$$\frac{d}{r} = \frac{r \cdot t}{r}$$

You can use this formula to find the number of seconds for Flight WAL27 to travel 30 feet to the **new** point where the two routes meet.

$$\text{Flight WAL27} \quad t = \frac{30 \text{ feet}}{0.5 \text{ feet per second}} = \underline{\hspace{2cm}} \text{ seconds}$$

(Hint: Divide 30 by 0.5 .)

Use the same formula to find the number of seconds for Flight NAL63 to travel 24 feet to the **new** point where the two routes meet.

$$\text{Flight NAL63} \quad \underline{\hspace{2cm}} \text{ seconds}$$



Name

$$t = d / r$$

Now answer these questions.

1. How many seconds will it take each plane to arrive at the new point where the two routes meet?

WAL27 _____ seconds

NAL63 _____ seconds

2. Will the two planes meet at the new point where the two routes come together? _____

3. Why or why not? _____

4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the new point where the routes come together? _____

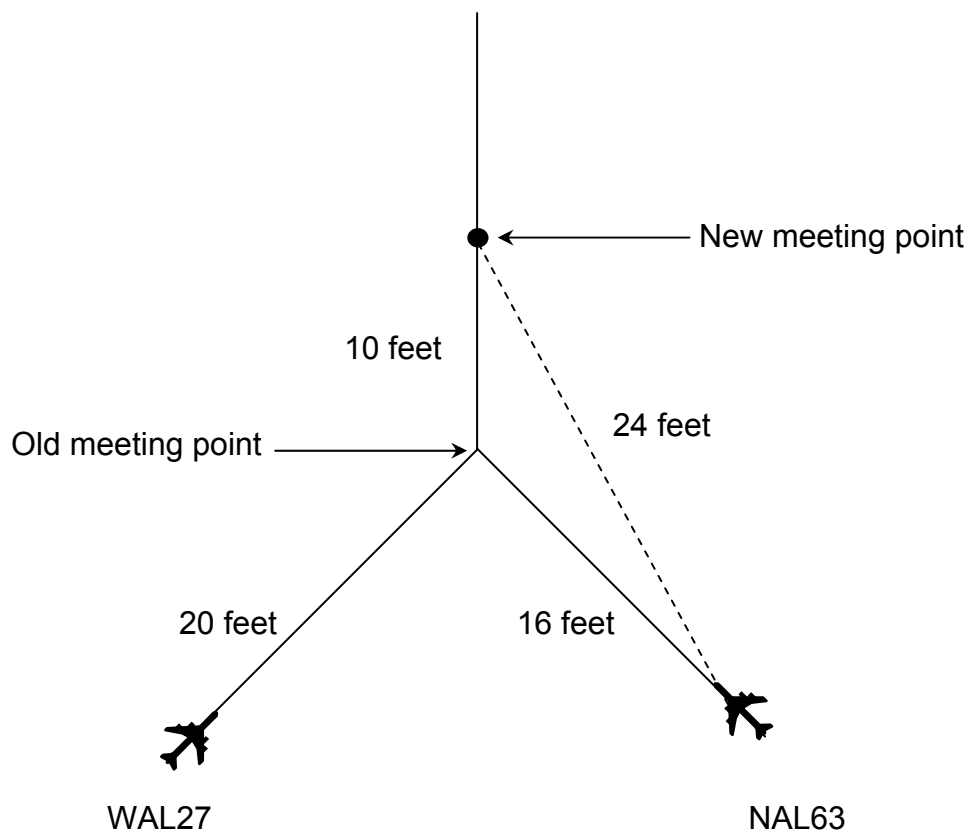
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the new point where the routes come together? _____

6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____



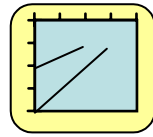
Name

$$t = d / r$$





Name



How Much Time To Reach the Point Where the Two Routes Meet? (Graph Two Linear Equations to Find the Answer)

We can use a linear equation to describe the position of an airplane that travels at a constant speed.

We begin with Flight WAL27.

The speed of Flight WAL27 is 0.5 feet per second.

When the clock starts at 0 seconds, the plane is 30 feet from the **new** point where the two routes meet.

The position of Flight WAL27 is given by this equation:

$$y = 0.5x - 30 \qquad \text{WAL27}$$

Here:

x = the time traveled (in seconds) and

y = the number of feet (with a negative sign attached)
from the intersection of the two routes.

Notice that when $x = 0$, $y = -30$.

This means that when the clock starts at 0 seconds, the plane is 30 feet from the point where the two routes meet.

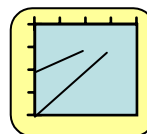
Now think about Flight NAL63.

The speed of Flight NAL63 is also 0.5 feet per second. However, its distance from the **new** intersection is 24 feet. So the position of Flight NAL63 is given by this equation:

$$y = 0.5x - 24 \qquad \text{NAL63}$$



Name



Complete each table and use the ordered pairs to graph each line.

WAL27 $y = 0.5x - 30$

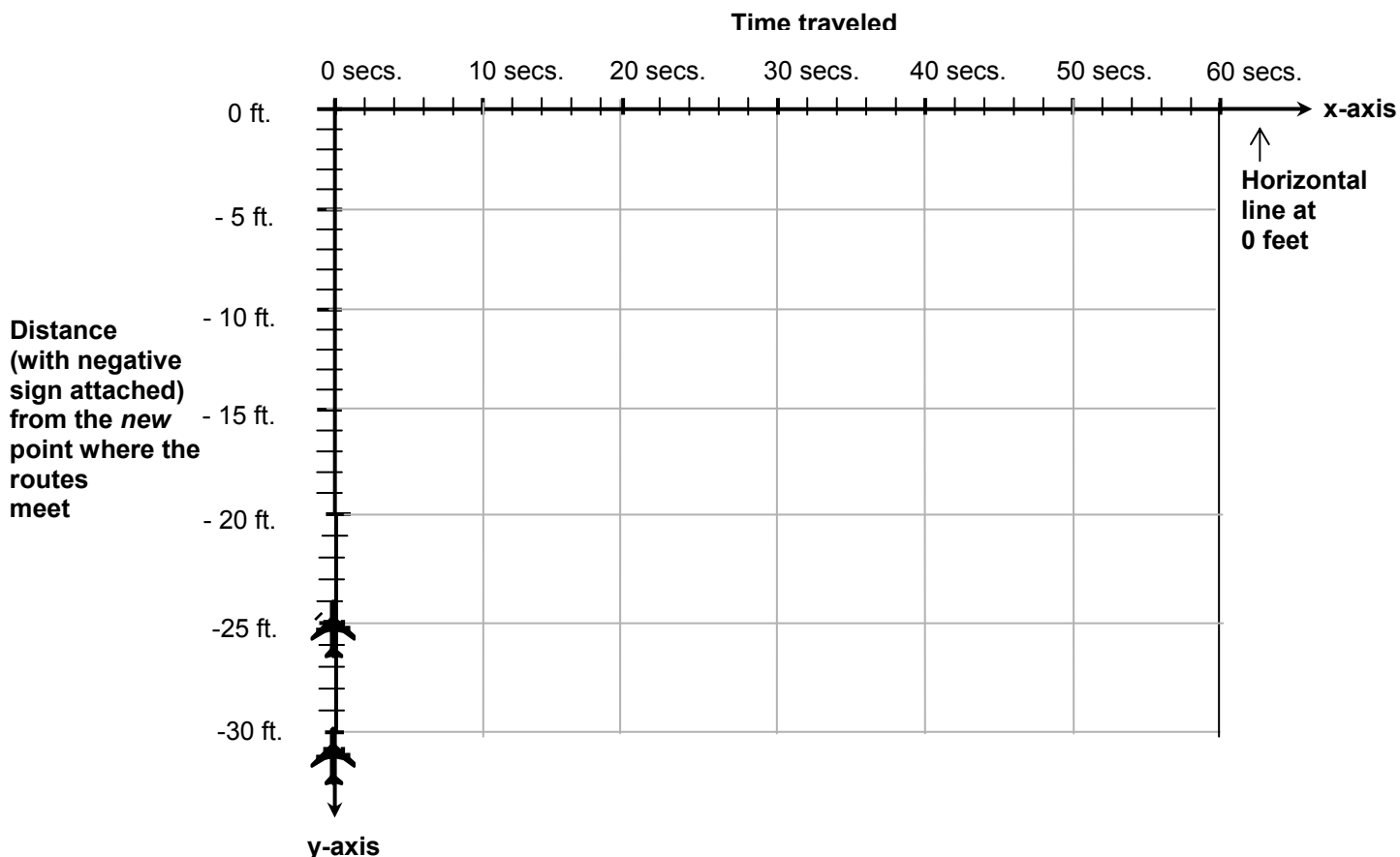
NAL63 $y = 0.5x - 24$

x	y
0	
10	
20	
30	
40	

x	y
0	
10	
20	
30	
40	

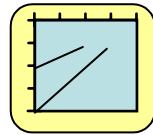
Use a solid line for the graph of **Flight WAL27**.

Use a dotted line for the graph of **Flight NAL63**.





Name



Use your graphs to answer the following questions.

1. How many seconds will it take each plane to arrive at the point where the two routes meet?

WAL27 _____ seconds

NAL63 _____ seconds

2. Will the two planes meet at the point where the two routes come together? _____

3. Why or why not? _____

4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together? _____

5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? _____

6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____

7. Write the number that is the slope of the solid line representing Flight WAL27. _____

8. Write the number that is the slope of the dotted line representing Flight NAL63. _____

9. What information does the slope of each line tell you about each plane?



Name

After the Experiment

Now you will compare your prediction with the results of the experiment.

First, circle your role in the experiment:

Pilot of WAL27	NASA Scientist for WAL27	Lead Air Traffic Controller
Pilot of NAL63	NASA Scientist for NAL63	Other Air Traffic Controller

Take a look at your prediction.

Did you predict the planes would meet at the new point where
the two routes come together?

Yes No

Next look at the results of the experiment.

Did the planes meet at the new point where the two routes
come together?

Yes No

Does your prediction match the experiment?

Yes No

If your answer to the last question is No, why do you think your prediction and the
experiment do not match? _____

Take another look at your prediction.

When the first plane gets to the new point where the routes meet, how many feet away
did you think the second plane would be?

Does your prediction match the experiment?

If your answer is No, why do you think your prediction and the experiment do not
match? _____



Name

Did the planes meet the 5-foot separation standard?

That is, were the planes at least 5 feet apart when the first plane reached the new point where the routes come together? _____

If planes did *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to meet the separation standard next time?

Take another look at the problem.

The speed of Flight WAL27 was $\frac{1}{2}$ foot per second.

The speed of Flight NAL63 was $\frac{1}{2}$ foot per second.

Were the speeds the same or different?

Same speed

Different speeds

Flight WAL27 started 30 feet from the new point where the routes come together.

Flight NAL63 started 24 feet from the new point where the routes come together.

When the planes started, what was their separation distance? That is, how much closer was Flight NAL63 to the new point where the routes come together? _____

What was the separation distance between the two planes when Flight NAL63 reached the new point where the routes come together? _____

How does the actual separation distance compare with the 5-foot separation standard?



Name _____

Now think about this general problem.

Two planes are traveling at the same speed on two different routes.

The planes are different distances from the point where the two routes come together.

Will the planes meet at the point where the routes come together? _____

How does the separation distance of the planes at the start compare with their separation distance at the point where the routes come together? _____

If the planes meet the separation standard at the start, will they meet the separation standard at the point where the routes come together? Why or why not?



Name _____

Posttest

In the picture below, two airplanes are flying on different routes.

The speed of Flight WAL27 is 1 foot/second.

Flight WAL27 is 30 feet from the **old** point where the two routes come together.

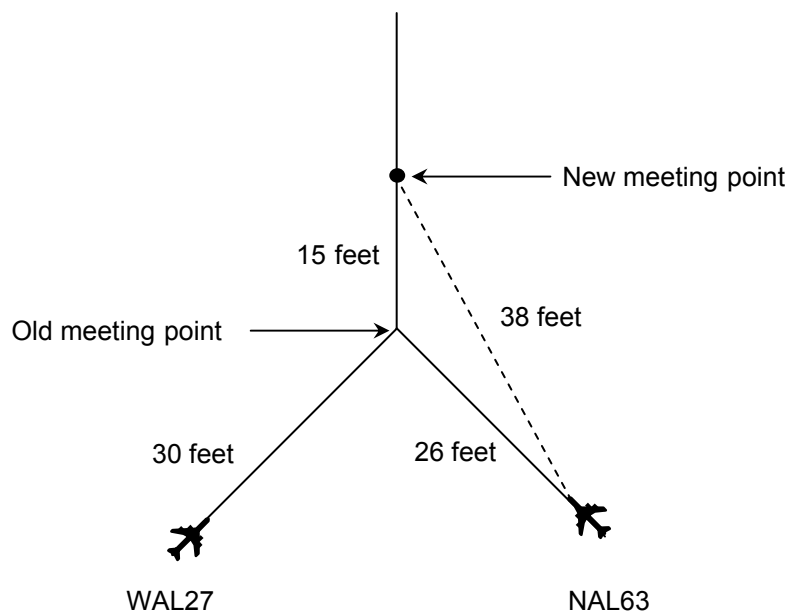
The speed of Flight NAL63 is 1 foot/second.

Flight NAL63 is 26 feet from the **old** point where the two routes come together.

The separation standard is 5 feet.

To prevent a separation violation, the air traffic controllers give Flight NAL63 a new, longer route. The new route is 38 feet long.

The new route is shown with a dotted line.





Name

1. Do you think that the two planes will meet at the **new** point where the two routes come together? _____

Why or why not? _____

2. If not, how far apart do you think the planes will be when the first plane reaches the new point where the routes come together? _____

3. Does your answer to Question 2 meet the 5-foot separation standard? _____

4. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? _____

Now consider this general problem.

Two planes are traveling at the same speed on two different routes.

The planes are different distances from the point where the two routes come together.

5. Will the planes meet at the point where the routes come together? _____

6. How does the separation distance of the planes at the start compare with their separation distance at the point where the routes come together?



Name

7. If the planes meet the separation standard at the start, will they meet the separation standard at the point where the routes come together? Why or why not?

Airspace Systems – Predicting Air Traffic Conflicts

Curriculum Supplement 4

ANSWERS & EXPLANATIONS

A note on the organization of the Answers and Explanations:

In this Curriculum Supplement, most of the activities pose the same set of questions. The answers to those questions are introduced in the first part of this answer document. The remainder of the document is organized by activity and includes answers to individual activity questions, graphs, applications of the distance-rate-time formula, and discussions of the general problems posed in the analysis activity and the posttest.

The speed of Flight WAL27 is 1/2 foot/second, so the plane travels 1/2 foot in 1 second. The speed of Flight NAL63 is 1/2 foot/second, so the plane travels 1/2 foot in 1 second. Flight WAL27 is 20 feet from the original point of intersection. Flight NAL63 is 16 feet from the original point of intersection. A 5-foot separation distance is required. If the separation becomes less than 5 feet, then a separation violation will occur.

Since the planes are traveling at the same constant (fixed) speed, the separation distance at the intersection will be the same as at the start. Since this separation is less than the separation standard, a separation violation will occur.

To avoid this, the air traffic controller uses an alternate 24-foot route for Flight NAL63 to try to resolve the separation violation. This results in a new point of intersection located 10 feet beyond the original intersection.

Given the alternate route:

- It will take 60 seconds for Flight WAL27 to travel 30 feet (20 feet plus 10 feet) to the new point where the routes come together.
- It will take 48 seconds for Flight NAL63 to travel 24 feet to the new point where the routes come together.
- At 48 seconds, when Flight NAL63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will be 6 feet apart when the first plane arrives at the new intersection and a separation violation will *not* occur.

Activity 4.3A—Count Feet and Seconds:

Each plane travels 1 foot in 2 seconds. Count by 2s to complete the table.

Flight WAL27 will travel 30 feet in 60 seconds. (Students can also multiply 2 seconds per foot by 30 feet to obtain 60 seconds.)

Flight NAL63 will travel 24 feet in 48 seconds. (Students can also multiply 2 seconds per foot by 24 feet to obtain 48 seconds.)

So Flight NAL63 arrives at the intersection 12 seconds ahead of Flight WAL27.

To determine the separation distance between the planes, note that 12 seconds at 1/2 foot/second corresponds to 6 feet. This separation is greater than the 5-foot separation standard. Therefore a separation violation does *not* occur.

1. Fill in the given table to see how many seconds it will take each plane to travel to the point where the two routes meet.

Flight WAL27		Flight NAL63	
How many feet?	How many seconds?	How many feet?	How many seconds?
1	2	1	2
2	4	2	4
3	6	3	6
4	8	4	8
5	10	5	10
6	12	6	12
7	14	7	14
8	16	8	16
9	18	9	18
10	20	10	20
11	22	11	22
12	24	12	24
13	26	13	26
14	28	14	28
15	30	15	30
16	32	16	32
17	34	17	34
18	36	18	36
19	38	19	38
20	40	20	40
21	42	21	42
22	44	22	44
23	46	23	46
24	48	24	48
25	50		
26	52		
27	54		
28	56		
29	58		
30	60		

Activity 4.3A (cont.)

2. How many seconds will it take each plane to arrive at the point where the two routes meet?

WAL27 60 seconds

NAL63 48 seconds

3. Will the two planes meet at the point where the two routes come together?

No

4. Why or why not? At 48 seconds, when Flight NAL 63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will not meet.

5. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together?

6 feet

6. Does your answer to Question 5 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? Yes.

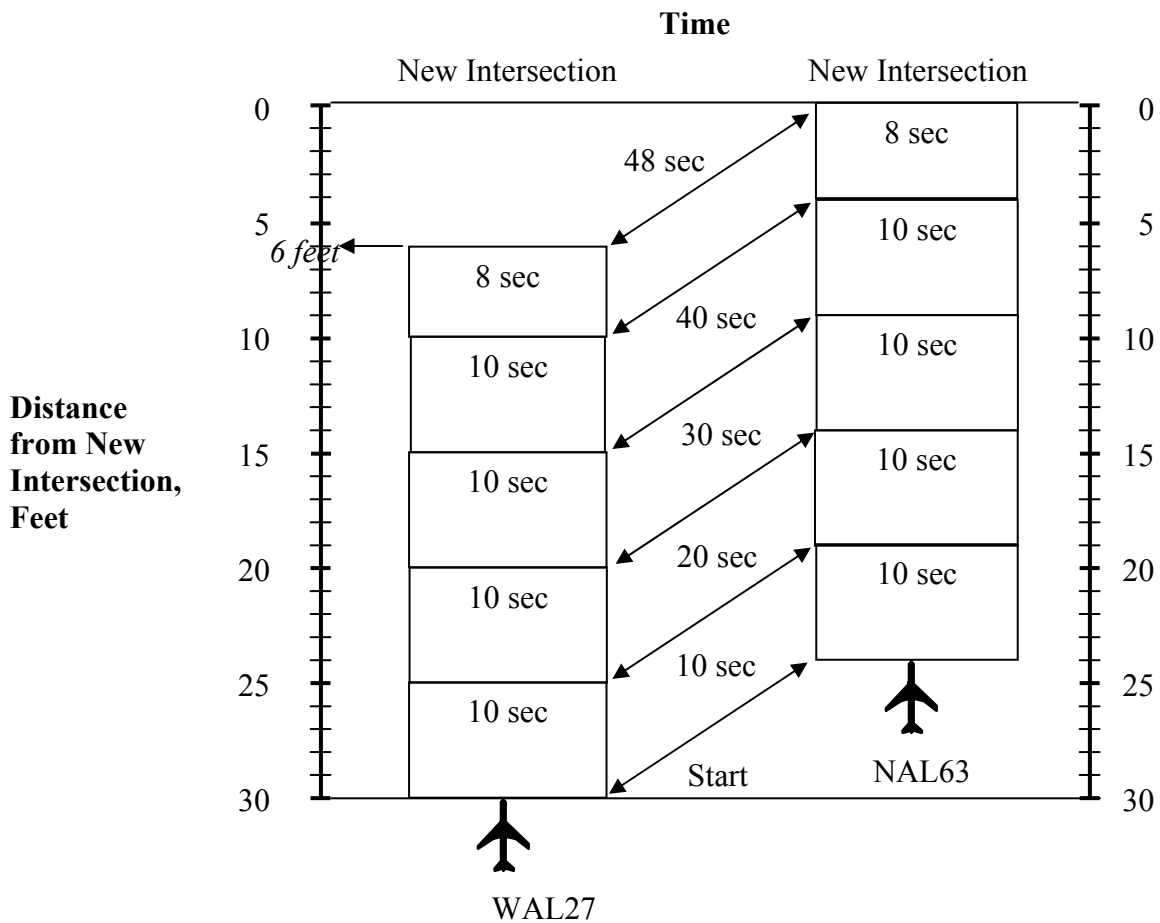
7. You filled in the table to find the answers. Can you think of a faster way to find the answer? If so, describe the faster way. For Flight WAL27, multiply 2 seconds per foot by 30 feet to obtain 60 seconds. For Flight NAL63, multiply 2 seconds per foot by 24 feet to obtain 48 seconds.

8. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? Change the speed or change the route of one of the planes.

Activity 4.3B—Stacking Blocks:

Each plane travels 1 foot in 2 seconds. So in 10 seconds, each plane will go 5 feet. The following diagram shows the 5-foot blocks added together. To get the answer in seconds, add the 10-second blocks.

As the blocks for Flight NAL63 are stacked, it will become clear that the answer is a little less than 50 seconds. In particular, Flight NAL63 has to go 4 feet past 40 seconds. This 4-foot distance corresponds to 8 seconds. So Flight NAL 63 will arrive at the new intersection in 48 seconds. At this time, Flight WAL27 is 6 feet from the new intersection. This distance is greater than the required 5-foot separation standard, so a separation violation will *not* occur.



1. Circle the flight number of the first plane to arrive at the new point where the two routes meet. How many seconds will it take that plane to arrive at the new point where the two routes meet?

WAL27 60 seconds

NAL63 48 seconds

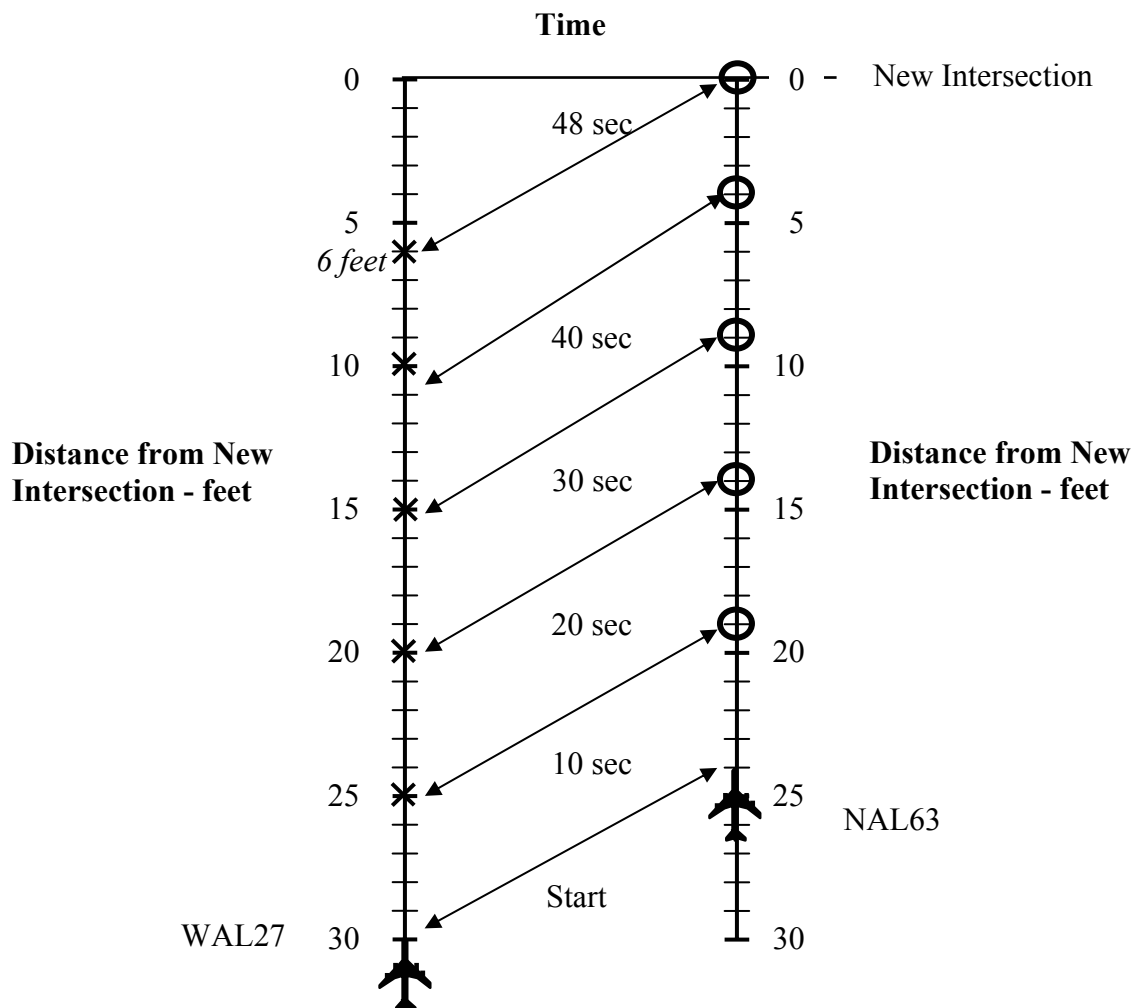
Activity 4.3B (cont.)

2. Will the two planes meet at the point where the two routes come together? No
3. Why or why not? At 48 seconds, when Flight NAL 63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will not meet.
4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together? 6 feet
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? Yes.
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? Change the speed or change the route of one of the planes.

Activity 4.3C—Plot Points on Lines:

Each plane travels 1 foot in 2 seconds. So in 10 seconds, each plane will go 5 feet. The following diagram shows the position of each plane at 10-second intervals.

As the points for Flight NAL63 are plotted, it will become clear that the answer is a little less than 50 seconds. In particular, Flight NAL63 has to go 4 feet past 40 seconds. This 4-foot distance corresponds to 8 seconds. So Flight NAL 63 will arrive at the new intersection in 48 seconds. At this time, Flight WAL27 is 6 feet from the new intersection. This distance is greater than the required 5-foot separation standard, so a separation violation will *not* occur.



Activity 4.3C (cont.)

1. Circle the flight number of the first plane to arrive at the new point where the two routes meet. How many seconds will it take that plane to arrive at the new point where the two routes meet?

WAL27 60 seconds

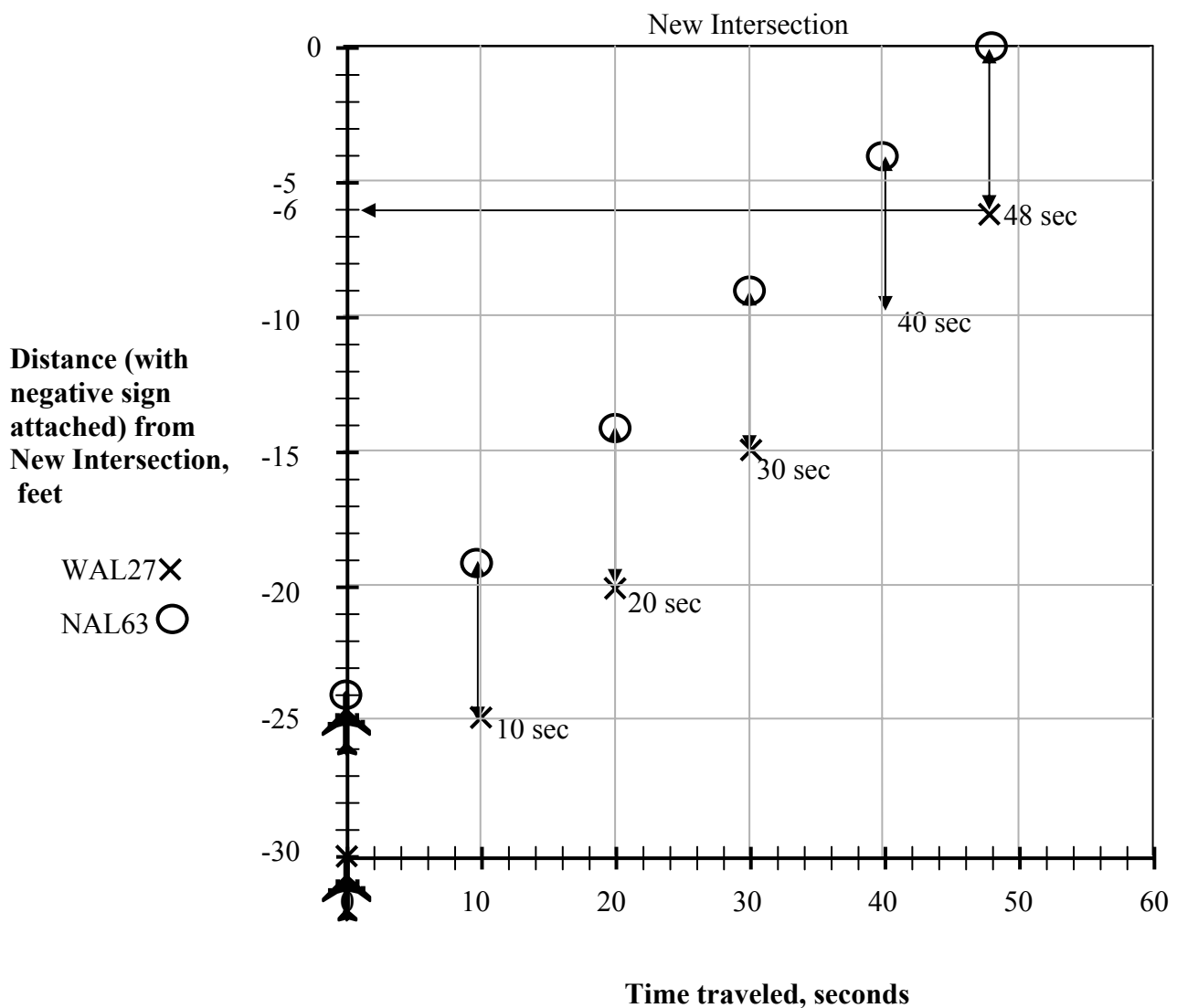
NAL63 48 seconds

2. Will the two planes meet at the point where the two routes come together? No
3. Why or why not? At 48 seconds, when Flight NAL 63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will not meet.
4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together? 6 feet
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? Yes.
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? Change the speed or change the route of one of the planes.

Activity 4.3D—Plot Points on a Grid:

Each plane travels 1 foot in 2 seconds. So in 10 seconds, each plane will go 5 feet. The following graph shows the position of each plane at 10-second intervals.

As the points for Flight NAL63 are plotted, it will become clear that the answer is a little less than 50 seconds. In particular, Flight NAL63 has to go 4 feet past 40 seconds. This 4-foot distance corresponds to 8 seconds. So Flight NAL 63 will arrive at the new intersection in 48 seconds. At this time, Flight WAL27 is 6 feet from the new intersection. This distance is greater than the required 5-foot separation standard, so a separation violation will *not* occur.



Activity 4.3D (cont.)

1. Circle the flight number of the first plane to arrive at the new point where the two routes meet. How many seconds will it take that plane to arrive at the new point where the two routes meet?

WAL27 60 seconds

NAL63 48 seconds

2. Will the two planes meet at the point where the two routes come together? No
3. Why or why not? At 48 seconds, when Flight NAL 63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will not meet.
4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together? 6 feet
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? Yes.
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? Change the speed or change the route of one of the planes.

Activity 4.3E—Derive the Distance-Rate-Time Formula:

In 4 seconds, each plane travels $0.5 \text{ feet/second} \times 4 \text{ seconds} = 2.0 \text{ feet}$.

In 5 seconds, each plane travels $0.5 \text{ feet/second} \times 5 \text{ seconds} = 2.5 \text{ feet}$.

In 6 seconds, each plane travels $0.5 \text{ feet/second} \times 5 \text{ seconds} = 3.0 \text{ feet}$.

To find the distance each plane travels in 14 seconds, multiply 0.5 feet/second by 14.

To find the distance each plane travels in 20 seconds, multiply 0.5 feet/second by 20.

The result is 10.0 feet.

1. In 4 seconds, each plane travels 0.5 feet/second \times 4 seconds = 2.0 feet.
2. In 5 seconds, each plane travels 0.5 feet/second \times 5 seconds = 2.5 feet.
3. In 6 seconds, each plane travels 0.5 feet/second \times 6 seconds = 3.0 feet.
4. How could you use multiplication to find the distance each plane travels in 14 seconds? Multiply 0.5 feet/second by 14 seconds.
5. Use the formula to find the distance traveled by each plane in 20 seconds.
In 20 seconds, each plane travels 10 feet.

Activity 4.3F—Use the Distance-Rate-Time Formula:

Calculate the time it takes each aircraft to travel to the new intersection.

The travel times are:

WAL27: $t = 30 \text{ feet} / 0.5 \text{ feet per second} = 60 \text{ seconds}$

NAL63: $t = 24 \text{ feet} / 0.5 \text{ feet per second} = 48 \text{ seconds}$

Flight WAL27 is 12 seconds behind Flight NAL63 when Flight NAL63 arrives at the new intersection. To find the corresponding distance, use the Distance-Rate-Time Formula in the form $d = r \cdot t$ with $r = 0.5 \text{ feet per second}$ and $t = 12 \text{ seconds}$.

$$d = r \cdot t = 0.5 \text{ feet/second} \times 12 \text{ seconds} = 6 \text{ feet}$$

This distance is greater than the required 5-foot separation standard, so a separation violation will *not* occur.

Flight WAL27 $t = \frac{30 \text{ feet}}{0.5 \text{ feet per second}} = \underline{60} \text{ seconds}$

(Hint: Divide 30 by 0.5 .)

Flight NAL63 $t = \frac{24 \text{ feet}}{0.5 \text{ feet per second}} = \underline{48} \text{ seconds}$

1. How many seconds will it take each plane to arrive at the point where the two routes meet?

WAL27 60 seconds

NAL63 48 seconds

2. Will the two planes meet at the point where the two routes come together?

No

3. Why or why not? At 48 seconds, when Flight NAL 63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will not meet.

Activity 4.3F (cont.)

4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together? 6 feet
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? Yes.
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? Change the speed or change the route of one of the planes.

Activity 4.3G—Graph Two Linear Equations:

Use the time (48 seconds) when Flight NAL63 arrives at the new intersection. On the line corresponding to Flight WAL27, locate the point where the time is 48 seconds. That point corresponds to a distance 6 feet from the intersection. This distance is greater than the 5-foot separation standard, so a separation violation will *not* occur.

$$\text{WAL27 } y = 0.5x - 30$$

x	y
0	-30
10	-25
20	-20
30	-15
40	-10

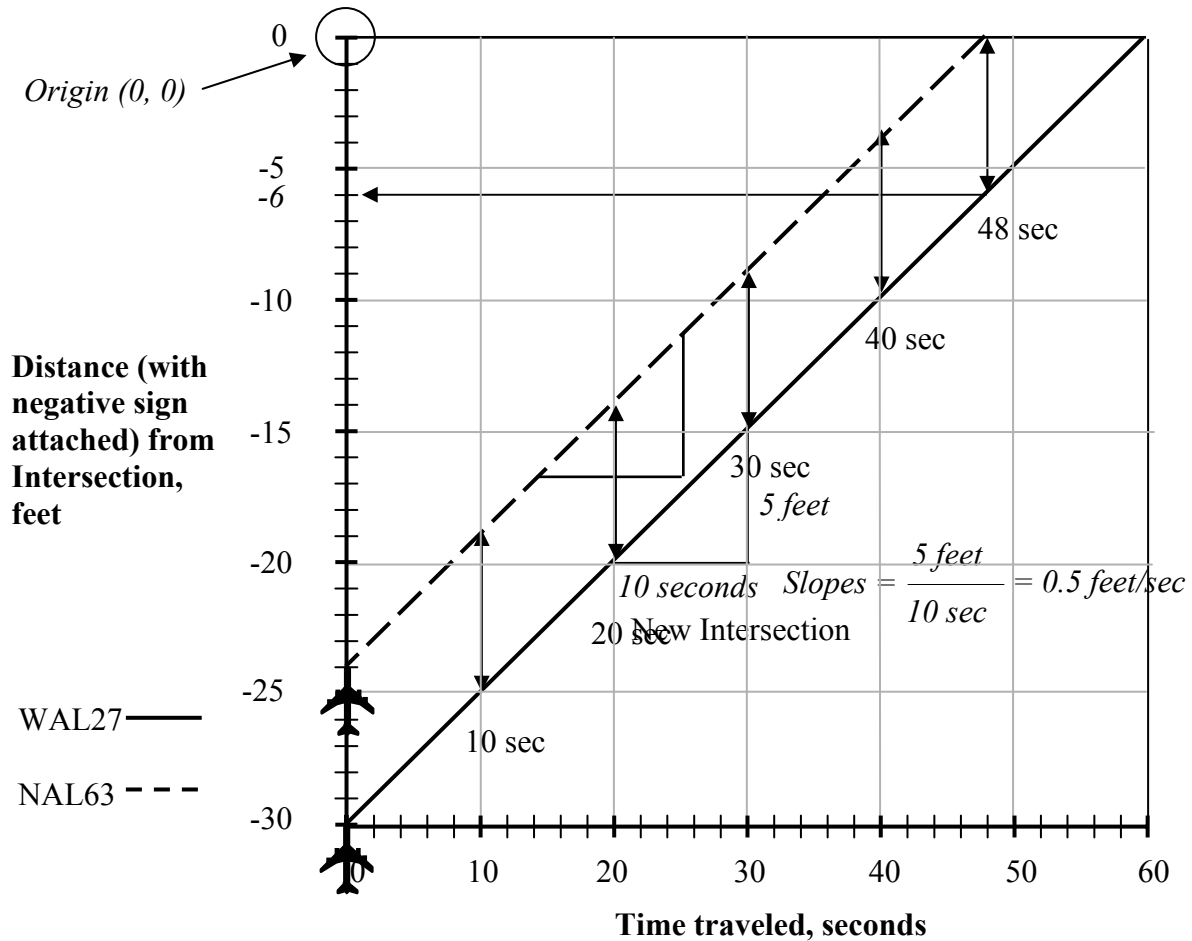
$$\text{NAL63 } y = 0.5x - 24$$

x	y
0	-24
10	-19
20	-14
30	-9
40	-4

The slope of each line is 0.5 feet/sec, the speed of each plane.
Since the lines have the same slope, the lines are parallel.

The vertical intercept of each line (-30 and -24, respectively) corresponds to each plane's initial distance (30 feet and 24 feet, respectively) from the new intersection.

Activity 4.3G (cont.)



- How many seconds will it take each plane to arrive at the point where the two routes meet?

WAL27 60 seconds

NAL63 48 seconds

- Will the two planes meet at the point where the two routes come together?

No

- Why or why not? At 48 seconds, when Flight NAL 63 arrives at the new intersection, Flight WAL27 will be 6 feet from the new intersection. So the planes will not meet.

Activity 4.3G (cont.)

4. If you think the planes will not meet, how many feet apart will the planes be when the first plane reaches the point where the routes come together? 6 feet
5. Does your answer to Question 4 meet the 5-foot separation standard? That is, do you think the planes will be at least 5 feet apart when the first plane reaches the point where the routes come together? Yes.
6. If you think the two planes will *not* meet the 5-foot separation standard, what could you tell the air traffic controllers to do to make sure that the separation standard will be met? Change the speed or change the route of one of the planes.
7. Write the number that is the slope of the solid line representing Flight WAL27. 0.5 feet/second
8. Write the number that is the slope of the dotted line representing Flight NAL63. 0.5 feet/second
9. What information does the slope of each line tell you about each plane?
The slope of each line is 0.5 feet/second, the speed of the plane.

Activity 4.4—After the Experiment and Activity 4.5—Posttest:

The plane speeds are the same.

The planes are different distances from the finish point.

When the planes started, their new separation distance was 6 feet. That is, Flight NAL63 was 6 feet closer to the new intersection than Flight WAL27. When Flight NAL63 reached the intersection, the separation distance was also 6 feet. This met the 5-foot separation standard.

General Problem:

Suppose two planes are traveling at the same speed on two different routes and the planes are different distances from the point where the two routes come together.

Since the planes are traveling at the same constant (fixed) speed and must each travel a different distance to the point of intersection, the planes will arrive at the intersection at different times.

Also, since the planes are traveling at the same constant (fixed) speed, their separation remains the same. So at the intersection, the separation between the planes will be the same as their initial separation. If the planes meet the separation standard at the start, they will meet the separation standard at the intersection.